


Parallax of a nearby star


Parallax of an even closer star

## Careful measurements of the parallaxes of stars reveal their distances

## Relation between a star's distance and its parallax

$$
d=\frac{1}{p}
$$

$d=$ distance to a star, in parsecs
$p=$ parallax angle of that star, in arcseconds

- Distances to the nearer stars can be determined by parallax, the apparent shift of a star against the background stars observed as the Earth moves along its orbit
- Parallax measurements made from orbit, above the blurring effects of the atmosphere, are much more accurate than those made with Earth-based telescopes
- Stellar parallaxes can only be measured for stars within a few hundred parsecs

If a star's distance is known, its luminosity can be determined from its brightness

Inverse-square law relating apparent brightness and luminosity

$$
b=\frac{L}{4 \pi d^{2}}
$$

```
b= apparent brightness of a star's light, in W/m
L = star's luminosity, in W
d= distance to star, in meters
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- A star's luminosity (total power of light output), apparent brightness, and distance from the Earth are related by the inverse-square law
- If any two of these quantities are known, the third can be calculated

Determining a star's luminosity from its apparent brightness

$$
\frac{L}{\mathrm{~L}_{\odot}}=\left(\frac{d}{\mathrm{~d}_{\odot}}\right)^{2} \frac{b}{\mathrm{~b}_{\odot}}
$$

$L / L_{\odot}=$ ratio of the star's luminosity to the Sun's luminosity
$d / \mathrm{d}_{\odot}=$ ratio of the star's distance to the Earth-Sun distance
$b / b_{\odot}=$ ratio of the star's apparent brightness to the Sun's apparent brightness

## Astronomers often use the magnitude scale to denote brightness

Introduced by Hipparchus 129 BC
The apparent magnitude, $m$, is an alternative quantity that measures a star's apparent brightness

A $1^{\text {st }}$ mag star is 100 times brighter than a $6^{\text {th }}$ mag star (definition).

Then a $1^{\text {st }}$ mag star is $\sqrt[5]{100}=2.512$ times brighter than a $2^{\text {nd }}$ mag star and (2.512) ${ }^{2}$ times brighter than a $3^{\text {rd }}$ mag star and ...

$$
m_{2}-m_{1}=2.5 \log \left(b_{1} / b_{2}\right)
$$

The absolute magnitude, M , of a star is the apparent magnitude it would have if viewed from a distance of 10 pc

$$
m-M=5 \log (d)-5
$$

M of Sun?
$M=-5 \log (d)+5+m$
$M=-5 \log (1 / 206265)+5+(-26.7)$
$M=4.8$


## $\longleftarrow$ Sun (-26.7)

ఒ Full moon (-12.6)
$\longleftarrow$ Venus (at brightest) (-4.4)
$\longleftarrow$ Sirius (brightest star) (-1.4)
$\longleftarrow$ Naked eye limit (+6.0)
$\longleftarrow$ Binocular limit (+10.0)
$\longleftarrow$ Pluto (+15.1)

Large telescope (visual limit) (+21.0)

Hubble Space Telescope and large Earth-
based telescopes (photographic limit) (+30.0)
Some apparent magnitudes

## Distance Modulus

- Consider a star with apparent magnitude, m, and absolute magnitude, M. Then
- $m-M=5 \log (d)-5$
- Note that d is in pc
- Further, if $\mathrm{d}=10 \mathrm{pc}$ then

$$
\begin{aligned}
m-M & =5 \log (10)-5 \\
m-M & =5-5 \\
& =0
\end{aligned}
$$

- $\mathrm{m}-\mathrm{M}$ is called the distance modulus

What would be the apparent magnitude of the Sun at $\mathrm{d}=120 \mathrm{pc}$ ?

$$
\begin{aligned}
m-M & =5 \log (d)-5 \\
m & =5 \log (120)-5+4.8 \\
m & =10.2
\end{aligned}
$$



Apparent magnitudes of stars in the Pleiades

$$
\mathrm{d}=120 \mathrm{pc}
$$

## A star's color depends on its surface temperature



The spectra of stars reveal their chemical compositions as well as surface temperatures

- Stars are classified
 into spectral types (subdivisions of the spectral classes O, B, A, F, G, K, and M), based on the major patterns of spectral lines in their spectra


## Spectra of stars with different T



Relationship between a star's luminosity, radius, and surface temperature

$$
L=4 \pi R^{2} \sigma T^{4}
$$

$L=$ star's luminosity, in watts
$R=$ star's radius, in meters
$\sigma=$ Stefan-Boltzmann constant $=5.67 \times 10^{-8} \mathrm{~W} \mathrm{~m}^{-2} \mathrm{~K}^{-4}$
$T=$ star's surface temperature, in kelvins

Stars come in a wide variety of sizes

## Finding Key Properties of Nearby Stars



## Hertzsprung-Russell (H-R) diagrams reveal the different kinds of stars

- The H-R diagram is a graph plotting the absolute magnitudes of stars against their spectral types-or, equivalently, their luminosities against surface temperatures
- The positions on the H-R diagram of most stars are along the main sequence, a band that extends from high luminosity and high surface temperature to low luminosity and low surface temperature



## The sizes of stars on an H-R diagram


$L=4 \pi R^{2} \sigma T^{4}$
$R=\left[L /\left(4 \pi \sigma T^{4}\right)\right]^{1 / 2}$
On the H-R diagram, giant and supergiant stars lie above the main sequence, while white dwarfs are below the main sequence

(a) A supergiant star has a low-density, low-pressure atmosphere:
its spectrum has narrow absorption lines

(b) A main-sequence star has a denser, higher-pressure atmosphere: its spectrum has broad absorption lines
By carefully examining a star's spectral lines, astronomers can determine whether that star is a main-sequence star, giant, supergiant, or white dwarf

## Using the H-R diagram

 and the inverse square law, the star'sluminosity and distance can be found without measuring its stellar parallax


## Surface temperature, T



- Ancient peoples looked at the stars and imagined groupings made pictures in the sky and gave them meaning.
- But they were on the wrong track.
- Today we look at the colours and get the surface temperature and the energy flux per $\mathrm{m}^{2}$.
- With the parallax and apparent brightness we get the luminosity and the radius.
- The life and death of stars


## Orion



The center of mass of the system of two children is nearer to the more


A "binary system" of two children


A binary star system

Binary star systems provide crucial information about stellar masses

- Binary stars are important because they allow astronomers to determine the masses of the two stars in a binary system
- The masses can be computed from measurements of the orbital period and orbital dimensions of the system

$$
M_{1}+M_{2}=\frac{a^{3}}{p^{2}}
$$

$M_{1}, M_{2}$ = masses of two stars in binary system, in solar masses $a=$ semimajor axis of one star's orbit around the other, in AU
$P=$ orbital period, in years


$L / L_{\text {sol }}=\left(M / M_{\text {sol }}\right)^{3.5}$
With: $\quad E / E_{\text {sol }}=L t /\left(L_{\text {sol }} t_{\text {sol }}\right)=\mathrm{fMc}^{2} /\left(\mathrm{fM}_{\text {sol }} \mathrm{C}^{2}\right)$
Lifetime on main sequence: $\left.\mathrm{t} / \mathrm{t}_{\text {sol }}=\mathrm{M} / \mathrm{M}_{\text {sol }}\right)^{-2.5}$
f: fraction of mass converted into energy


## $\mathrm{L} / \mathrm{L}_{\text {sol }}=\left(\mathrm{M} / \mathrm{M}_{\text {sol }}\right)^{3.5}$ Lifetime on main sequence: $\left.\mathrm{t} / \mathrm{t}_{\text {sol }}=\mathrm{M} / \mathrm{M}_{\text {sol }}\right)^{-2.5}$

$\mathrm{E} / \mathrm{E}_{\text {sol }}=\mathrm{Lt} /\left(\mathrm{L}_{\text {sol }} \mathrm{t}_{\text {sol }}\right)=\mathrm{fMc} \mathrm{C}^{2} /\left(\mathrm{fM}_{\text {sol }} \mathrm{C}^{2}\right)$

