

Part One

Here are the constants and other values we require

$$> \text{metabolic} := 5 \frac{[\text{J}]}{[\text{kg}][\text{s}]} : \text{weight} := 0.0005[\text{kg}] : \text{glucose} := 0.00066 \frac{[\text{mol}]}{[\text{liter}]} : \text{Gibbs} := 2870 \cdot 10^3 \frac{[\text{J}]}{[\text{mol}]} :$$

Now we can solve for the liters of xylem sap required per second

$$> \frac{\text{metabolic} \cdot \text{weight}}{\text{glucose} \cdot \text{Gibbs}}$$
$$\frac{1.32 \times 10^{-6} [\text{L}]}{[\text{s}]} \quad (1)$$

To determine the time required for the insect to 'drink' its body weight, divide weight (as volume) by the xylem consumption rate.

$$> \frac{0.0005 [\text{L}]}{1.32 \times 10^{-6} [\text{L}]} \frac{[\text{s}]}{[\text{s}]}$$
$$378.7878788 [\text{s}] \quad (2)$$

Thus, the insect must drink its body weight every 6.3 minutes!
Scoring: equation set-up (6/10); correct answers (2/10 and 2/10)

Part Two

Here are the constants and values we require (T = 293 K)

$$> RT := 2.437 \frac{[\text{liter}][\text{MPa}]}{[\text{mol}]} :$$

For phloem cells, the internal pressure can be estimated to be

$$> \text{solve} \left(P = RT \cdot 1 \frac{[\text{mol}]}{[\text{liter}]}, P \right)$$
$$2.44 \times 10^0 [\text{MPa}] \quad (3)$$

For xylem cells, the internal pressure can be estimated to be

$$> \text{solve} \left(P = RT \cdot 0.001 \frac{[\text{mol}]}{[\text{liter}]}, P \right)$$
$$2.44 \times 10^{-3} [\text{MPa}] \quad (4)$$

>
Thus, a phloem-feeding insect doesn't have to pump, because the internal pressure is so high (2.44 MPa).
By contrast, a xylem-feeding insect does.... The cell osmotic pressure is low, and the xylem is normally under suction (about 2000 kPa).

To do so, it has to have a pump strong enough to 'suck' the solution.

This in turn means the insect has to be large enough to provide for the pump muscles (Cibarial dilator muscles).

This is why xylem-feeding insects are larger than their phloem-feeding counterparts.

Scoring: equation set-up and/or correct analysis (10/10). The constants provided were incorrect. This is accounted for in scoring.