# AS/ECON 4070A Public Finance I Assignment 1 

due: Wednesday October 112000 before class

Answer all 5 questions. All count equally.

1. Would the allocation resulting from the following economic system be Pareto efficient? Explain briefly.

The economic system : there are two goods in the economy, food and clothing ; there is no production ; goods are allocated by competitive markets ; people buy and sell the two goods, taking the prices of the goods as given ; each person has a given endowment of food and clothing ; there is a government, which takes 25 percent of any clothing sold ; the clothes taken by the government are distributed, in equal shares, to all the people in the economy ; the government does nothing else, except for taking and redistributing clothing.
2. Suppose that a person's utility function, from consumption of two goods, had the equation

$$
U(x, y)=x y
$$

where $x$ was her consumption of one good, and $y$ her consumption of the other, so that, for instance, her indifference curve through the consumption bundle $(12,12)$ is the set of all consumption bundles $(x, y)$ such that $x y=144$.

Suppose that initially the prices of the two goods are $p_{x}=p_{y}=1$, and that the person's income is 24 . Suppose as well that the person chose the bundle $(12,12)$ initially. Then a tax on $\$ 1.25$ per unit on good $Y$ raises $p_{y}$ to $\$ 2.25$. The person then chooses the consumption bundle (12, $5 \frac{1}{3}$ ).
$i$ Check that $(12,12)$ is the consumer's preferred consumption bundle if her income is 24 , and if the prices she faces for the two goods are ( 1,1 ), and that $\left(12,5 \frac{1}{3}\right)$ is her preferred consumption bundle if her income is 24 and if the prices she faces are $(1,2.25)$.
$i i$ How much would she be willing to pay to avoid the tax on good $Y$ ? (That is, what is the equivalent variation to the tax? )
iii How much would she have to be compensated, in order to undo the damage done by the tax? ( That is, what is the compensating variation for the tax? )
3. What would the incidence be of a $\$ 6$ unit tax on cigars, if the market for cigars were perfectly competitive, if the demand curve for cigars had the equation

$$
Q^{D}=180-2 P^{D}
$$

where $Q^{D}$ is the quantity demanded by consumers and $P^{D}$ the price paid by buyers, and if the quantity supplied of cigars were

$$
Q^{s}=4 p_{s}
$$

where $Q^{s}$ is the quantity supplied by sellers and $p_{s}$ is the price received by sellers?
4. A perfectly price discriminating monopoly charges a different price for each unit sold. ( "First degree price discrimination" is another way of saying "perfect price discrimination".) A perfectly price discriminating monopoly charges buyers exactly the maximum the buyers are willing to pay for each unit of the good sold.
$i$ What would be the incidence of a unit tax levied on the monopoly, of $\$ 1$ for each unit that it sold?
ii What would be the incidence of the $\$ 1$ unit tax, if it were levied on buyers of the good?
5. Suppose firms in some industry set prices by using a simple "mark-up" rule. That is, they set the price of the good they sell equal to the average cost of the good, plus some positive fraction $m$ of this average cost.
$i$ What would be the incidence of a $\$ 1$ unit tax, levied on all firms in this industry, on each unit sold?
ii What would be the incidence of this $\$ 1$ unit tax, if it were levied on buyers of the good?

