AS/ECON 4070A Public Finance I Assignment 1

due : Wednesday October 11 2000 before class

Answer all 5 questions. All count equally.

1. Would the allocation resulting from the following economic system be Pareto efficient? Explain briefly.

The economic system : there are two goods in the economy, food and clothing ; there is no production ; goods are allocated by competitive markets ; people buy and sell the two goods, taking the prices of the goods as given ; each person has a given endowment of food and clothing ; there is a government, which takes 25 percent of any clothing sold ; the clothes taken by the government are distributed, in equal shares, to all the people in the economy ; the government does nothing else, except for taking and redistributing clothing.

2. Suppose that a person's utility function, from consumption of two goods, had the equation

$$U(x,y) = xy$$

where x was her consumption of one good, and y her consumption of the other, so that, for instance, her indifference curve through the consumption bundle (12, 12) is the set of all consumption bundles (x, y) such that xy = 144.

Suppose that initially the prices of the two goods are $p_x = p_y = 1$, and that the person's income is 24. Suppose as well that the person chose the bundle (12, 12) initially. Then a tax on \$1.25 per unit on good Y raises p_y to \$2.25. The person then chooses the consumption bundle $(12, 5\frac{1}{3})$.

i Check that (12, 12) is the consumer's preferred consumption bundle if her income is 24, and if the prices she faces for the two goods are (1, 1), and that $(12, 5\frac{1}{3})$ is her preferred consumption bundle if her income is 24 and if the prices she faces are (1, 2.25).

ii How much would she be willing to pay to avoid the tax on good Y? (That is, what is the *equivalent variation* to the tax?)

iii How much would she have to be compensated, in order to undo the damage done by the tax? (That is, what is the *compensating variation* for the tax?)

3. What would the incidence be of a \$6 unit tax on cigars, if the market for cigars were perfectly competitive, if the demand curve for cigars had the equation

$$Q^D = 180 - 2P^D$$

where Q^D is the quantity demanded by consumers and P^D the price paid by buyers, and if the quantity supplied of cigars were

$$Q^s = 4p_s$$

where Q^s is the quantity supplied by sellers and p_s is the price received by sellers?

4. A perfectly price discriminating monopoly charges a different price for each unit sold. ("First degree price discrimination" is another way of saying "perfect price discrimination".) A perfectly price discriminating monopoly charges buyers exactly the maximum the buyers are willing to pay for each unit of the good sold.

i What would be the incidence of a unit tax levied on the monopoly, of \$1 for each unit that it sold?

ii What would be the incidence of the \$1 unit tax, if it were levied on buyers of the good?

5. Suppose firms in some industry set prices by using a simple "mark–up" rule. That is, they set the price of the good they sell equal to the average cost of the good, plus some positive fraction m of this average cost.

i What would be the incidence of a \$1 unit tax, levied on all firms in this industry, on each unit sold?

ii What would be the incidence of this \$1 unit tax, if it were levied on buyers of the good?