time : 50 minutes

Do all 3 questions. All count equally.

1. Suppose that for some people (but not for all people) there was some maximum amount $\bar{Z}$ of a public good which they wished to consume. For quantities above $\bar{Z}$, these people receive no additional benefit.

Would it ever be efficient to provide a quantity of this public good which is greater than $\bar{Z}$ ? Explain.
2. Describe briefly a tax mechanism which would induce people to reveal truthfully how much they are willing to pay for a single "all or nothing" public project.
3. Suppose that firms 1 and 2 both sell their outputs on competitive markets, at a price of $\$ 1$ per unit of output sold. Suppose as well that each firm could hire labour at a wage of $\$ 10$ per hour, and buy coal at $\$ 10$ per tonne.

Firm 1's output, as a function of its use $L_{1}$ of labour and $Z_{1}$ of coal, is

$$
F^{1}\left(L_{1}, Z_{1}\right)=\ln L_{1}+210 Z_{1}-\left(Z_{1}\right)^{2}
$$

while firm 2's output, as a function of its own labour use $L_{2}$, and firm 1's coal use $Z_{1}$, is

$$
F^{2}\left(L_{2}, Z_{1}\right)=\ln L_{2}-\left(Z_{1}\right)^{2}
$$

(where "ln" refers to the natural logarithm function).
How much coal would firm 1 use, if it had to compensate firm 2 for any damage its coal use imposed, if the two firms were able to negotiate with each other?

