a social choice rule is **strategy-proof** if it is **never** a good strategy to misrepresent your rankings

misrepresentation is a good idea, for some profile of voters' preferences, and some social choice rule, if

I like x better than y

for this profile, the social choice rules chooses y

but if I reported some other ranking (not true ranking), then the social choice rule will choose  $\mathbf{x}$ 

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## A Social Choice Rule is "Onto" if ..

for any alternative x , there exists some profile of preferences for which the rule will pick x

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**THEOREM** : If a social choice rule is strategy–proof and onto, then it must be dictatorial.

(proof in 2 stages)

*Proposition i* : If a social choice rule is "monotonic", and if it obeys the Pareto principle, then it must be dictatorial.

*Proposition ii* : If a social choice rule is strategy–proof and onto, then it must be monotonic, and it must satisfy the Pareto principle.

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