#### (cf. Persson and Tabellini, pp. 104–108)

# different from simple "pairwise majority rule" : legislature has an **agenda**

only a limited number of proposals can be made

#### Framework

"standard" *Persson–Tabellini* framework : policy is a level *g* of government spending people have single–peaked preferences high–income people prefer lower *g* 

except now there are only **3** income groups, and one party for each income group

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 $y_L < y_M < y_R$  (so that  $g_L^* > g_M^* > g_R^*$ )

one party gets to propose a policy

if no proposal is passed, the default "reversion" policy  $\bar{g}$  implemented

no single group (L, M or R) has a majority of voters, so a policy needs the support of at least 2 groups — any 2 — to pass

# 1 Stage

some party is (randomly) chosen to make a proposal that party introduces some policy g if the proposing party, and one other party (or both other parties) vote for the proposal, then g is implemented if both opposition parties votes against the proposed g, then the reversion policy  $\overline{g}$  is implemented

[so "yes" is a vote for the proposal g, and "no" is a vote for the reversion policy  $\bar{g}$ ]

if the middle party gets to propose, then it can get its most-preferred policy  $g_M$  passed

why? if  $\bar{g} > g_M$ , then single–peakedness says that party R votes for  $g_M$  (over  $\bar{g}$ )

and if  $\bar{g} < g_M$ , then single–peakedness says that party *L* votes for  $g_M$  (over  $\bar{g}$ )

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## 1 Stage, government is L

single–peakedness says that party L must get the support of party M to pass its proposals

case 1 :  $g_L < \bar{g}$  : *M* prefers  $g_L$  to  $\bar{g}$ , so party *L* proposes its most–preferred policy (and gets it passed)

case 2 :  $g_M < \bar{g} < g_L$  : the highest level of spending that party *L* can get passed is  $\bar{g}$  (so it proposes the reversion level  $\bar{g}$  and gets it passed)

case 3 :  $\bar{g} < g_M$  : find  $\tilde{g}_M > g_M$  which leaves party *M* indifferent between  $\bar{g}$  and  $\tilde{g}_M$ 

that's the largest level of spending which can passed and party *L* will propose that  $\tilde{g}_M$  (unless  $\tilde{g}_M$  is actually even bigger than what party *L* wants, in which case it proposes  $g_L$ ) so that the policy chosen (and passed) is min( $\tilde{g}_M, g_L$ )

#### 2 Stages

now : one party (of  $\{L, M, R\}$ ) is chosen to make an initial proposal  $g_1$ 

if  $g_1$  passes, that's it

if  $g_1$  is defeated, we go to a second stage in the second stage, some **other** party (one of the remaining 2) gets to propose some  $g_2$  and that  $g_2$  goes up against  $\overline{g}$ 

#### second stage

if we ever get to the second stage, it's exactly like the one-stage bargaining :

in any 2nd stage, the proposal does get passed, and

party *M* proposes  $g_M$ , party *L* proposes  $g_L$ , or  $\bar{g}$  or the biggest g which can defeat  $\bar{g}$ , party *R* proposes  $g_R$ , or  $\bar{g}$  or the smallest g which can defeat  $\bar{g}$ 

and all 3 parties can anticipate that this will happen if the initial proposal  $g_1$  is defeated in the first stage

### The "Continuation" Game

let  $\hat{g}_i$  denote the proposal that party i ( $i \in \{L, M, R\}$ ) proposes (and gets passed) in the 1–stage model which is also the proposal party i will propose, if it gets the chance, in the second stage of the 2–stage model

if  $p_i$  is the probability that party i ( $i \in \{L, M, R\}$ ) gets to make the proposal in the second stage (if we do get to a second stage)

then the outcome of the second stage will be  $\hat{g}_L$  with probability  $p_L$ ,  $\hat{g}_M = g_M$  with probability  $p_M$  and  $\hat{g}_R$  with probability  $p_R$  — if we get to a second stage and let  $\beta < 1$  indicate how much people value the future

so (for example), if the initial proposal (in the first stage) is defeated, party *M*'s expected value from the resulting second stage is

$$V_M = \beta [\rho_L W_M(\hat{g}_L) + \rho_M W_M(\hat{g}_M) + \rho_R W_M(\hat{g}_R)]$$
(1)

which means that party M would vote for some initial 1st-stage proposal (by L or R)  $g_1$  if and only if

 $W_M(g_1) \ge V_M = \beta [p_L W_M(\hat{g}_L) + p_M W_M(\hat{g}_M) + p_R W_M(\hat{g}_R)]$  (2)

they need party *M*'s vote to get that proposal passed so they will propose the largest  $g_1$  that satisfies (2)

[that result depends on

1. party L wants to get party M's support initially, not party R's

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2. party *L* wants to have its 1st–stage proposal passed

both these statements are true here]

### if party *M* gets the initial proposal ...

then they can get their preferred policy  $g_M$  passed in the initial stage (for sure)

*proof* : let  $Eg_2$  be the expected value of the policy which would be chosen in the second stage, if we were to get there :

$$Eg_2 \equiv \rho_L \hat{g}_L + \rho_M \hat{g}_M + \rho_R \hat{g}_R \tag{3}$$

if voters are risk-averse, then for any party *i*,

$$V_i = \beta E W_i(g_2) \le \beta W_i(Eg_2) \le W_i(Eg_2)$$
(4)

so any party would rather have  $Eg_2$  (for sure), then have the vote go to a second stage

if  $Eg_2 > g_M$ , then

party *R* prefers  $g_M$  to  $Eg_2$ , and prefers  $Eg_2$  to having the vote go to a second stage so party *R* would then vote in favour of  $g_M$  in the firsts stage

but if  $Eg_2 < g_M$ , then party *L* prefers  $g_M$  to  $Eg_2$ , and prefers  $Eg_2$  to having the vote go to a second stage so party *L* would then vote in favour of  $g_M$  in the first stage

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if party *L* gets to choose the policy in period 1, then it will not necessarily have to choose  $g_M$  to get its policy passed

but if  $p_M$  is high, and  $\beta$  close to 1, it will have to choose a policy close to  $g_M$ 

[since then party *M* will want to go to a second stage, unless the first–stage policy is almost as attractive to them as  $g_M$ ]

### Many Stages

if we have more than 2 stages, then party *M* will still choose its most–preferred policy  $g_M$  whenever it gets the chance so with many stages, the policy is very likely to get to  $g_M$  which means that the initial policy must be very close to  $g_M$  when there are many stages — if  $\beta$  is not too low