GS/ECON 5010 Assignment 4 F2006

due: Wednesday November 22 before class

Do all 5 questions. Each counts 20%.

1. What does the contract curve look like for a 2-person, 2-good exchange economy, with a total endowment of 60 units of good 1 and 120 units of good 2, if the preferences of the two people could be represented by the utility functions

$$u^{1}(x_{1}^{1}, x_{2}^{1}) = \ln x_{1}^{1} + 2 \ln x_{2}^{1}$$

$$u^2(x_1^2, x_2^2) = 112 - \frac{1}{x_1^2} + \ln x_2^2$$

where x_j^i is person i's consumption of good j?

2. What are all the allocations in the core of a 3-person, 2-good economy, in which each person's preferences can be represented by the utility function

$$u^i(x_1^i, x_2^i) = x_1^i x_2^i$$

where x_j^i is person i's consumption of good j, and where the endowments e^i of the three people are $e^1 = (2,0)$, $e^2 = (0,2)$, $e^3 = (1,1)$?

- 3. Calculate the competitive equilibrium for the 2-person, 2-good economy described in question #1, if person 1's endowment was (0,30), and person 2's endowment was (60,90).
- 4. What are the core allocations to the economy described in question #2 above if, instead of 3 people, there were 3N people, N of each type, where N is large? (That is, all people have the same utility function, N of them have the endowment vector e^1 , N of them have the endowment vector e^2 , and N of them have the endowment vector e^3 .)

over

5. Find all the pure–strategy Nash equilibria in the following strategic–form two–person game.

LLLRRR(8, 8)(3, 5)(2, 4)(0, 1)ttt(8,3) (9,4)(4,0)(2, 2)b(6,5) (1,2)(6, 4)(5,0)bb(4,4) (0,8) (3,8) (10,7)