GS/ECON 5010 Assignment 4 F2008due : Friday November 21 8:30 amDo all 5 questions. Each counts 20%.

1. What does the contract curve look like for a 2-person, 2-good exchange economy, with a total endowment of 60 units of good 1 and 29 units of good 2, if the preferences of the two people could be represented by the utility functions

$$u^{1}(x_{1}^{1}, x_{2}^{1}) = \ln x_{1}^{1} + \ln x_{2}^{1}$$
$$u^{2}(x_{1}^{2}, x_{2}^{2}) = \ln x_{1}^{2} + x_{2}^{2}$$

where x_{i}^{i} is person *i*'s consumption of good *j*?

2. What are all the allocations in the core of a 3–person, 2–good economy, in which each person's preferences can be represented by the utility function

$$u^i(x_1^i, x_2^i) = 100 - \frac{1}{x_1^i} - \frac{1}{x_2^i}$$

where x_j^i is person *i*'s consumption of good *j*, and where the endowments e^i of the three people are $e^1 = (2,0), e^2 = (0,2), e^3 = (0,2)$?

3. What would the competitive equilibrium be in the economy described in question #1 above, if person 1's endowment of goods 1 and 2 was $\mathbf{e}^1 = (40, 18)$ and person 2's endowment was $\mathbf{e}^2 = (20, 11)$?

- 4. What is the competitive equilibrum to the economy described in question #2?
- 5. Find all the Nash equilibria in the following strategic-form two-person game.

| | a | b | c | d | e | f |
|----------|------------------------------------|---------------------|----------------|----------------|----------------|-------------------|
| $B \\ C$ | (3,0) (2,0) (6,12) (4,12) | $(1, 20) \\ (0, 4)$ | (8,0) (4,5) | (2,2) (6,6) | (4,8) (8,6) | (1, 18) (5, 7) |
| D | (4, 18) | (3,5) | (0, 8) | (8, 6) | (5, 12) | (4, 20) |