due: Friday November 21 8:30 am
Do all 5 questions. Each counts $20 \%$.

1. What does the contract curve look like for a $2-$ person, 2 -good exchange economy, with a total endowment of 60 units of good 1 and 29 units of good 2 , if the preferences of the two people could be represented by the utility functions

$$
\begin{gathered}
u^{1}\left(x_{1}^{1}, x_{2}^{1}\right)=\ln x_{1}^{1}+\ln x_{2}^{1} \\
u^{2}\left(x_{1}^{2}, x_{2}^{2}\right)=\ln x_{1}^{2}+x_{2}^{2}
\end{gathered}
$$

where $x_{j}^{i}$ is person $i$ 's consumption of good $j$ ?
2. What are all the allocations in the core of a 3-person, 2-good economy, in which each person's preferences can be represented by the utility function

$$
u^{i}\left(x_{1}^{i}, x_{2}^{i}\right)=100-\frac{1}{x_{1}^{i}}-\frac{1}{x_{2}^{i}}
$$

where $x_{j}^{i}$ is person $i$ 's consumption of good $j$, and where the endowments $e^{i}$ of the three people are $e^{1}=(2,0), e^{2}=(0,2), e^{3}=(0,2)$ ?
3. What would the competitive equilibrium be in the economy described in question $\# 1$ above, if person 1's endowment of goods 1 and 2 was $\mathbf{e}^{1}=(40,18)$ and person 2 's endowment was $\mathbf{e}^{2}=(20,11) ?$
4. What is the competitive equilibrum to the economy described in question $\# 2$ ?
5. Find all the Nash equilibria in the following strategic-form two-person game.

|  | $a$ | $b$ | $c$ | $d$ | $e$ | $f$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |
| $A$ | $(3,0)$ | $(12,5)$ | $(7,2)$ | $(4,19)$ | $(2,16)$ | $(3,14)$ |
| $B$ | $(2,0)$ | $(1,20)$ | $(8,0)$ | $(2,2)$ | $(4,8)$ | $(1,18)$ |
| $C$ | $(6,12)$ | $(0,4)$ | $(4,5)$ | $(6,6)$ | $(8,6)$ | $(5,7)$ |
| $D$ | $(4,18)$ | $(3,5)$ | $(0,8)$ | $(8,6)$ | $(5,12)$ | $(4,20)$ |

