Do all 5 questions. Each counts $20 \%$.

1. Are the preferences described below strictly monotonic? Convex? Explain briefly.

There are 3 different commodities. The person finds bundle $\mathbf{x}^{1}$ at least as good as bundle $\mathbf{x}^{2}$ if and only if : the minimum of $x_{1}^{1}$ and $\max \left(x_{2}^{1}, x_{3}^{1}\right)$ is at least as big as the minimum of $x_{1}^{2}$ and $\max \left(x_{2}^{2}, x_{3}^{2}\right)$. (Where max $(a, b)$ denotes the maximum of $a$ and $b$.)
2. Are the preferences represented by the utility function below strictly monotonic? Convex? Explain briefly.

$$
U\left(x_{1}, x_{2}, x_{3}\right)=\frac{x_{1}}{x_{1}+x_{2}}-\frac{1}{x_{3}}
$$

3. Calculate a person's Marshallian demand functions, if her preferences can be represented by the utility function

$$
u\left(x_{1}, x_{2}, x_{3}\right)=x_{1}\left(x_{2}+x_{3}\right)^{2}
$$

4. Calculate a person's Marshallian demand functions, if her preferences can be represented by the utility function

$$
u\left(x_{1}, x_{2}\right)=\frac{x_{1} x_{2}}{x_{2}+1}
$$

5. Find the expenditure function, Hicksian demand functions and indirect utility function for the preferences of question \#4 above.
