${\rm due: Monday\ November\ 28 \quad \ before\ class}$ 

Do all 5 questions. Each counts 20%.

1. What does the contract curve look like for a 2-person, 2-good exchange economy, if the preferences of the two people could be represented by the utility functions

$$u^{1}(x_{1}^{1}, x_{2}^{1}) = 100 - \frac{1}{x_{1}^{1}} - \frac{1}{x_{2}^{1}}$$

$$u^2(x_1^2, x_2^2) = x_2^2 + 100 \ln x_1^2$$

where  $x_j^i$  is person i's consumption of good j?

2. What are all the allocations in the core of a 3-person, 2-good economy, in which each person has the same endowment vector,  $e^i = (1,1)$ , and in which the preferences of the 3 people can be represented by the utility functions listed below?

$$u^1(x_1^1, x_2^1) = x_1^1$$

$$u^2(x_1^2, x_2^2) = x_2^2$$

$$u^3(x_1^3, x_2^3) = x_1^3 + x_2^3$$

3. How would the equilibrium prices of the goods vary with the people's endowments in a 2–person, 2–good exchange economy, if each person's preferences could be represented by the utility function

$$u^{i}((\mathbf{x}^{i}) = -\frac{1}{x_{1}^{i}} - \frac{1}{x_{2}^{i}}$$

where  $x_j^i$  was person i's consumption of good j?

continued over

4. Find all the pure–strategy Nash equilibria in the following strategic–form two–person game.

5. Find all the Nash equilibria (in pure or mixed strategies) to the following two–person game in strategic form.

$$\begin{array}{cccc} & L & R \\ t & (12,6) & (6,4) \\ m & (0,8) & (7,12) \\ b & (2,2) & (8,4) \end{array}$$