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Review (→ in-class exam #1 on 2/27, covering Giordano ch. 17-20)

- understand class notes
- understand text (key chapter sections noted on course webpage)
- tutorial problems
- HW problems

□ Have covered a wide range of topics so far, so we'll try to distill down the key concepts into a salient narrative here

## □ Electric Forces + Fields (ch. 17)

• charge is a fundamental property of matter

• protons, electrons, ions, ... →  $e = 1.60 \times 10^{-19} \text{ C}$

• charge exerts force on charge → Coulomb's Law  
$$\vec{F} = \frac{q_1 q_2}{4\pi\epsilon_0 r^2} \hat{r} = k \frac{q_1 q_2}{r^2} \hat{r} \quad \left( \begin{array}{l} \epsilon_0 = 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{N}\cdot\text{m}^2} \\ k = 9.0 \times 10^9 \frac{\text{N}\cdot\text{m}^2}{\text{C}^2} \end{array} \right)$$

• superposition of forces → remember that force is a vector (magnitude and direction)

• notion of a dipole (+ and - charge separated by a fixed dist.)

• notion of an electric field (think of analogy to gravity!)

$$\vec{F} = q\vec{E} \quad (\vec{E} \text{ is a vector; } q \text{ is a 'test charge'})$$

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- Conductors vs. Insulators: How does charge move about?
- Electric Flux (think of water/pipe analogy!)

$$\begin{aligned}\Phi_E &= \vec{E} \cdot \vec{A} \quad (\text{dot product, } \vec{A} \text{ is area vector}) \\ &= EA \cos \theta\end{aligned}$$

→ notion of a 'surface'

• Gauss' Law:  $\Phi_E = \sum \vec{E} \cdot d\vec{A} = \oint_S \vec{E} \cdot d\vec{A} = \frac{Q_{\text{enclosed}}}{\epsilon_0}$

↑  
'sum over a closed surface'

↑  
charge contained inside the closed surface

→ when symmetries exist (e.g. we can choose a surface over which  $\vec{E} \cdot d\vec{A}$  is const./zero), Gauss' Law gives us a powerful tool for calculating electric fields

NOTE: remember that Gauss' Law sums the flux over the entire surface of the closed shape

## 2) Electric Potential (ch. 18)

- energy stored as a result of electrostatic forces (think analogy to gravitational potential energy)
- potential energy is energy 'stored' due to work

eg. energy between two point charges:  $U_{12} = k \frac{q_1 q_2}{r}$

[things to think about: conservation of energy, superposition, conservative forces, ...]

• Potential energy vs. 'potential':  $V(\vec{r}) = \frac{U_{el}(\vec{r})}{q_0}$  ← 'test charge'

→ potential is created by some distribution of charge, but we often describe it in terms of how it would affect an (arbitrary) 'test charge'

→ we call  $V$  a 'voltage'

• Distinction between a 'potential' ( $V$ ) and a 'potential difference' ( $\Delta V$ )

→ a reference is sometimes important (hence the need for 'ground' when dealing w/ circuits)

• Field lines (e.g. equipotential lines)

• Capacitors  $\Delta V = \frac{Q}{C}$  ( $C = \frac{\epsilon_0 A}{d}$  for p.p. capac.)

- storage of energy ( $U_{el} = \frac{1}{2} C \Delta V^2 = \frac{1}{2} \frac{Q^2}{C}$ )
- different geometries (e.g. parallel-plates)
- dielectrics ( $C = k_0 C_0$ )
- capacitors in series vs. parallel

→ think in analogy to a mechanical spring

### 3 Electric Circuits (ch. 19)

• Current ( $I = \frac{dq}{dt}$ ) → has a clearly defined direction

NOTE: positive charge moving L to R is same as negative charge R to L

• Battery: creates a potential difference (think of escalator analogy)

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$$R = \rho \frac{L}{A}$$

- Resistance (R)
  - conduction electrons and drift velocity → material property
  - resistivity ( $\rho$ )
  - notion of an 'ideal wire'

- Ohm's Law:  $\Delta V = IR$  → resistance leads to power dissipation! ( $P = I^2 R = I \Delta V = \frac{V^2}{R}$ )

- Circuit Basics
  - ideal wires
  - junctions
  - circuit elements: batteries, resistors, capacitors
  - notion of 'ground'
  - elements in series vs. parallel
  - voltmeter, current meter (ammeter)
  - resistors in series, parallel

Kirchoff's Laws

a) Junction Law:  $\sum I_{in} = \sum I_{out}$  (Conservation of charge)

b) Loop Law:  $\Delta V_{loop} = \sum_i \Delta V_i = 0$  (conservation of energy)

→ practice, practice, practice! Also make sure its clear how these 'laws' relate to changes in electric potential as one moves around a circuit

RC circuits → things can now change w/ time!

- simple RC circuit in series:  $\Delta V_B - IR - \frac{Q}{C} = 0$

where  $V_c(t) = \frac{Q(t)}{C}$   
 →  $I(t) = I_0 e^{-t/\tau}$  ( $\tau = RC$ )

# A1 Magnetism (ch. 20)

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- basics of magnets - field lines flow in loops
  - no magnetic monopoles (i.e. there is always a S end and a N)
  - earth has a magnetic field  $\rightarrow$  compass
  - certain materials are 'magnetic' (e.g. iron)
  - [etc....] incl. electromagnets

- Current-carrying  $\rightarrow$  magnetic field
  - Right-hand rule (RHR)
  - convention for drawing things ( $\times$  = into page, etc....)

- Ampère's Law
  - means to determine  $|\vec{B}|$  (magnetic field 'strength')
  - notion of a 'line integral'

$$\sum_{\text{closed path}} B_{\parallel} \Delta L = \oint_c \vec{B} \cdot d\vec{s} = \mu_0 I_{\text{enclosed}}$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A} \quad (\text{permeability of free space})$$

$\rightarrow$  provides us w/ a means to determine the magnetic field strength (given certain symmetries are satisfied, otherwise the math can be difficult)

- Loops vs. coils vs. solenoids vs. straight wire:  $B_{\text{wire}} = \frac{\mu_0 I}{2\pi r}$

$$B_{\text{loop}} = \frac{\mu_0 I}{2R}$$

$$B_{\text{coil}} = N \frac{\mu_0 I}{2R}$$

$$B_{\text{solenoid}} = \frac{\mu_0 NI}{L} \quad (L \gg R)$$

- Magnetic forces  $\rightarrow$  cross-product use RHR #2!  $\vec{F}_m = q(\vec{v} \times \vec{B})$ 
  - current carrying wires
  - moving charges in magnetic field
  - Hall effect