PHYS 1410: PHYSICAL SCIENCE (FW 2012/2013)

Additional problem for Oct. 30

Consider an object that moves on a circular path. Starting from the position vector $\vec{r}(t)$ show that the acceleration can be written as

$$\vec{a}(t) = \vec{a}_c(t) + \vec{a}_t(t)$$

with

$$a_{c} = \left(\frac{d\theta}{dt}\right)^{2} R$$
$$a_{t} = \left|\frac{d^{2}\theta}{dt^{2}}\right| R.$$

Note: consult Sec. 2.6 of the Math Addendum if you have problems with the chain rule.

- 1. Show that $a_c = \frac{v^2}{R}$ (where v is the speed of the object). Is a_c a constant or does it change with time?
- 2. Show that $a_t = \left| \frac{dv}{dt} \right|$. Is a_t a constant or does it change with time?
- 3. Show that $\vec{a}_c \perp \vec{a}_t$ (at all times)¹.
- 4. Show that $a_t = 0$ for the special case of *uniform* circular motion.