# Biophysics I (BPHS 4080)

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Website: http://www.yorku.ca/cberge/4080W2018.html

York University Winter 2018 Lecture 25

Reference/Acknowledgement: - TF Weiss (Cellular Biophysics) - D Freeman

$$\frac{1}{2\pi a(r_o + r_i)} \frac{\partial^2 V_m}{\partial z^2} = C_m \frac{\partial V_m}{\partial t} + G_K(V_m, t) (V_m - V_K) + G_{Na}(V_m, t) (V_m - V_{Na}) + G_L(V_m - V_L)$$

$$G_K(V_m, t) = \overline{G}_K n^4(V_m, t)$$

$$G_{Na}(V_m, t) = \overline{G}_{Na} m^3(V_m, t) h(V_m, t)$$

$$n(V_m, t) + \tau_n(V_m) \frac{dn(V_m, t)}{dt} = n_\infty(V_m)$$

$$m(V_m, t) + \tau_m(V_m) \frac{dm(V_m, t)}{dt} = m_\infty(V_m)$$

$$h(V_m, t) + \tau_h(V_m) \frac{dh(V_m, t)}{dt} = h_\infty(V_m)$$

$$\tau_{x}\frac{dx}{dt} + x = x_{\infty} \qquad \frac{dx}{dt} = \alpha_{x}(1-x) - \beta_{x}x$$
$$x_{\infty} = \alpha_{x}/(\alpha_{x} + \beta_{x}) \text{ and } \tau_{x} = 1/(\alpha_{x} + \beta_{x})$$

$$\begin{aligned} \alpha_m &= \frac{-0.1 \left( V_m + 35 \right)}{e^{-0.1 \left( V_m + 35 \right)} - 1}, \\ \beta_m &= 4e^{-(V_m + 60)/18}, \\ \alpha_h &= 0.07e^{-0.05 \left( V_m + 60 \right)}, \\ \beta_h &= \frac{1}{1 + e^{-0.1 \left( V_m + 30 \right)}}, \\ \alpha_n &= \frac{-0.01 \left( V_m + 50 \right)}{e^{-0.1 \left( V_m + 50 \right)} - 1}, \\ \beta_n &= 0.125e^{-0.0125 \left( V_m + 60 \right)}, \end{aligned}$$



#### Four phases:

- 1. Local disturbance due to capacitance (behaves like cable model)
- 2. Onset:  $V_m$  change triggers m(increased  $G_{Na}$  take  $V_m$  with it)
- 3. Falloff: *h* turns off, *n* turns on (both work to lower  $V_m$  back towards  $V_k$ , basis for absolute refractory period)
- 4. Undershoot: increased  $G_k$  pushes  $V_m$ beyond  $V_m^{o}$ (basis for relative refractory period)

<u>Note</u>: Membrane current  $(J_M)$  can be parsed up into two components: a capacitive current  $(J_C)$  and an ionic current  $(J_{ion})$ 



<u>Note</u>: Fairly little net current across membrane (i.e., relatively few net ions transported)

#### **Threshold**



# → What is mechanism for a threshold?

<u>Note</u>: Model is deterministic and does not capture stochastic behaviors manifest in-vivo

**Threshold** 

```
Space-clamped
```



→ Note lag for AP to occur (stems from capacitive build-up to threshold)



Determine  $J_{ion}$ - $V_m$  relationship right after shock (dashed line)

Current purely due to  $C_m$ 

Membrane "deciding" whether to fire AP or not

50

 $V_m - V_m^o (\mathrm{mV})$ 

100

$$J_{ion} = -J_C = -C_m \frac{dV_m}{dt}$$

Figure 4.43

![](_page_7_Figure_0.jpeg)

![](_page_7_Figure_1.jpeg)

# Equilibrium points

> Stability 
$$J_{ion} = -J_C = -C_m \frac{dV_m}{dt}$$

# > Threshold

> Ohm' s Law: Negative resistance?

![](_page_7_Figure_6.jpeg)

![](_page_8_Figure_0.jpeg)

![](_page_9_Figure_0.jpeg)

![](_page_10_Figure_0.jpeg)

#### <u>Threshold</u>: Phase Plane Portrait

![](_page_11_Figure_1.jpeg)

zoomed-in

 $\dot{m} = 0$ ,  $\dot{m} = 0$ ,  $\dot{W} = 0$ ,  $\dot{V} = V_m(t) - V_m^o \text{ (mV)}$ ,

assumes n and h are constant, but m varies dynamically

![](_page_11_Figure_5.jpeg)

## **Refractory Period**

![](_page_12_Figure_1.jpeg)

Figure 4.52

## Back to the question of spatial propagation...

![](_page_13_Figure_1.jpeg)

![](_page_14_Figure_1.jpeg)

![](_page_15_Figure_1.jpeg)

Figure 4.30

→ Solutions only stable for appropriate choice of conduction velocity

think back to cable model;  $C_m$  matters!)

![](_page_15_Figure_5.jpeg)

# Propagated APs

![](_page_16_Figure_1.jpeg)

![](_page_17_Figure_0.jpeg)

Similar picture as before for propagated AP

→ Note lag between  $V_m$  and  $G_m$  (stems from capacitive surge)

![](_page_18_Figure_0.jpeg)

 $\rightarrow$  Note lag between  $V_m$  and  $G_m$ 

(stems from capacitive surge)

# **Myelination**

![](_page_19_Figure_1.jpeg)

![](_page_20_Figure_0.jpeg)

![](_page_20_Picture_1.jpeg)

![](_page_20_Picture_2.jpeg)

Figure 5.5

![](_page_20_Picture_4.jpeg)

Figure 5.6

![](_page_20_Picture_6.jpeg)