

**SC/MATH 1019B - HOMEWORK 2**  
**DUE NOVEMBER,20 2018**

*Solutions to the problems below must be brought to class on November,20 2018. Solutions may be typed or neatly hand written. You must clearly indicate which problem you are solving. All solutions must be fully justified.*

# 1. Let  $\Sigma = \{a, b, c\}$ . Find a recurrence for the number of length  $n$  strings in  $\Sigma^*$  that do not contain any two consecutive  $a$ 's,  $b$ 's, nor  $c$ 's (i.e. none of  $aa$ ,  $bb$ , nor  $cc$  are in the string).

# 2. Solve the recurrence  $a_n = 5a_{n-1} - 6a_{n-2}$  where  $a_0 = 2$  and  $a_1 = 5$ .

# 3. Consider the relation  $R$  on  $\mathbb{Z} \times (\mathbb{Z} \setminus \{0\})$  defined by

$$R = \{((a, b), (c, d)) : ad = bc\}.$$

Prove that  $R$  is an equivalence relation. Does the relation  $R$  have any meaning to you?