

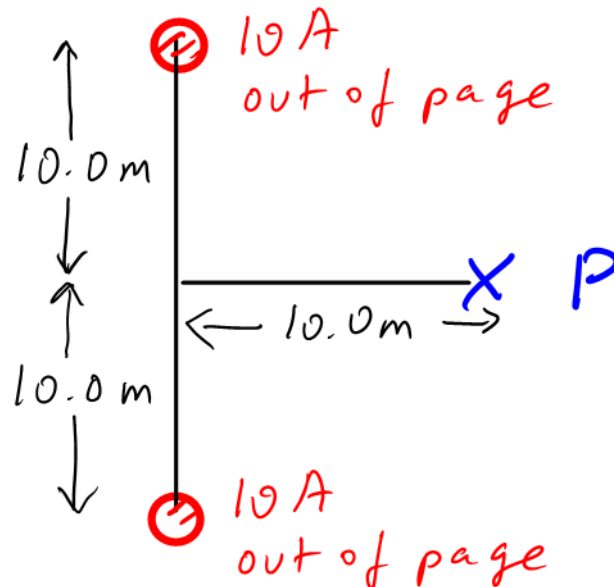
# PhysicsTutor<sup>mh</sup>

Magnetic field

Giambattista 19.99

# Problem:

- Two conducting wires perpendicular to the page are shown in cross section as red dots in the figure. They each carry 10.0 A out of the page. What is the magnetic field at point  $P$ ?



Relevant ideas:

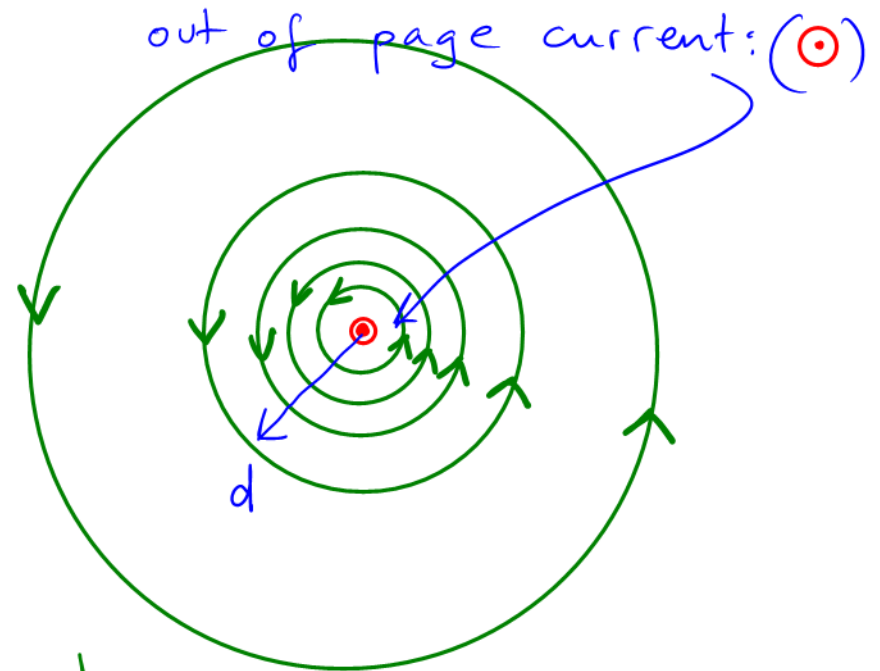
# Relevant ideas:

- A long current-carrying wire is surrounded by a magnetic field whose strength drops as  $1/d$ .

$$B = \frac{\mu_0 I}{2\pi d}$$

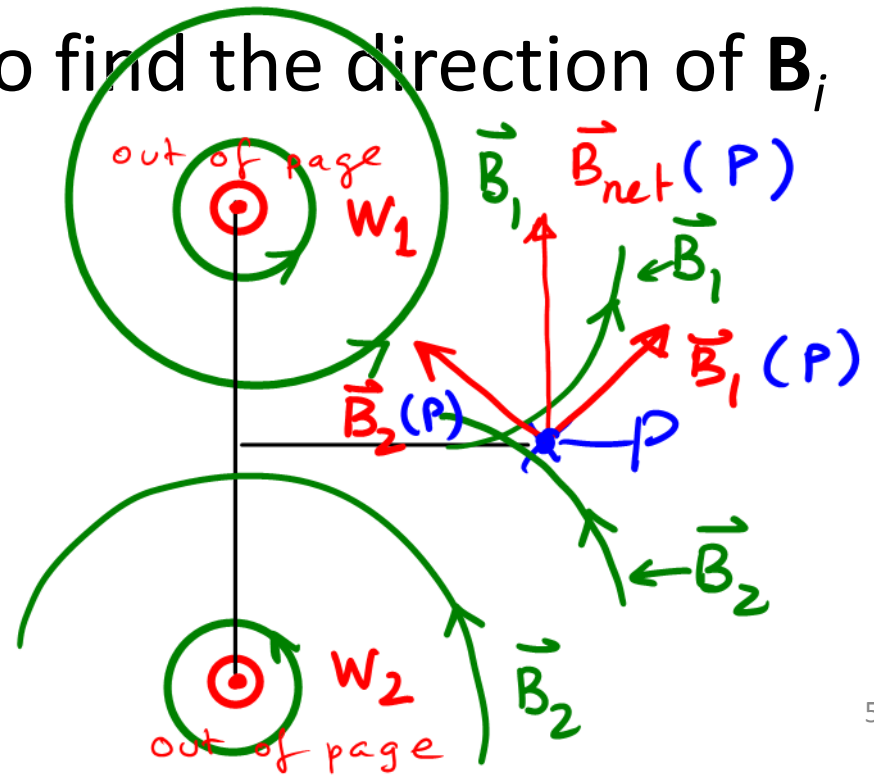
strength of  
B falls  
off with  
distance d

Spacing of field  
lines  
grows with d.



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- A long current-carrying wire is surrounded by a magnetic field whose strength drops as  $1/d$ .
- The field lines are circles about the wire. Use the Right-Hand rule to find the direction of  $\vec{B}_i$  at  $P$  for wires  $i = 1, 2$ .



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- A long current-carrying wire is surrounded by a magnetic field whose strength drops as  $1/d$ .
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- The net magnetic field adds all contributions.

vector addition required!

Do not add:  $B_1 = \frac{\mu_0 I}{2\pi d_1}$  and  $B_2 = \dots$

# Equations associated with ideas:

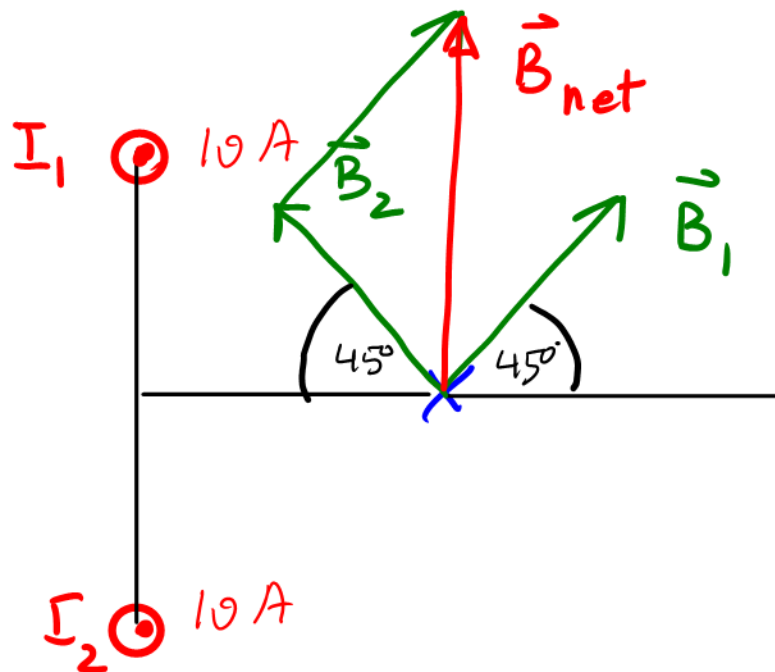
$$B = \frac{\mu_0 I}{2\pi d}$$

$$B_i = \frac{\mu_0 I_i}{2\pi d_i}$$

$$I_1 = I_2 = I$$

$$i = 1, 2$$

$$d_1 = d_2$$



$$B_{\text{net}}^2 = 2 B_1^2$$

since  $\vec{B}_1, \vec{B}_2$

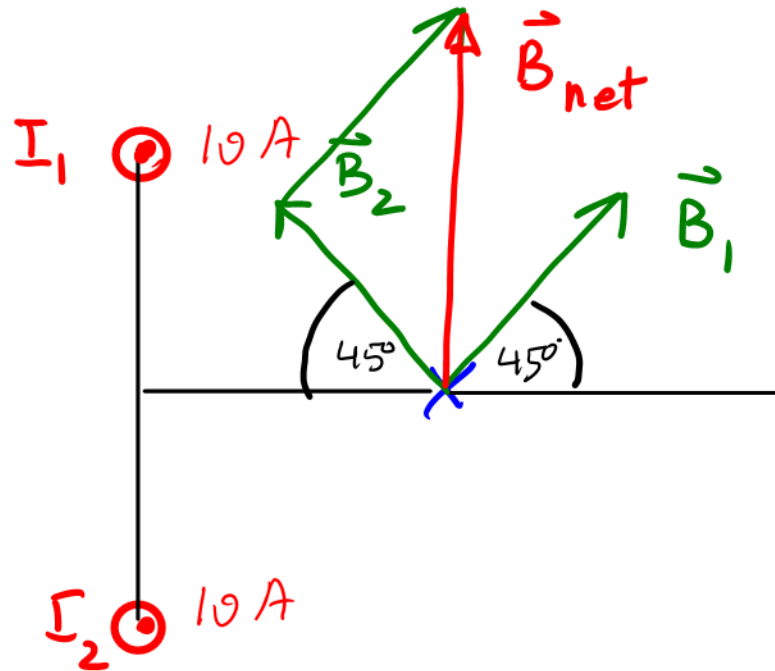
form a square

# Strategy



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- The net magnetic field at  $P$  is pointing up: the horizontal components cancel.
- Use vector addition: the magnetic field strength formula yields the magnitudes of  $\mathbf{B}_1$  and  $\mathbf{B}_2$ . The components are obtained from trigonometry (or geometry).

# Solution

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- $B_1 = \frac{\mu_0 I}{2\pi d_1}$  ;  $d_1 = \sqrt{10.0^2 + 10.0^2} \text{ m} = 14.1 \text{ m}$

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- $\vec{B}_{\text{net}} = 2.0 \times 10^{-7} \text{ T } \hat{j}$  ; upward direction

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