## PhysicsTutor

## Point charges: electric field

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## Problem:

- Two point particles with charges $q_{1}$ and $q_{2}$ are separated by a distance $L$, as shown. The electric field vanishes at $A$, which is a distance $L / 4$ from $q_{1}$. What is the ratio $q_{1} / q_{2}$ ?


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- Electric fields for multiple charges add vectorially (superposition principle). Total E represents net force divided by probe charge.
- Field from 2 charges is zero at some inbetween point: there must be a cancellation. The probe charge is in equilibrium there.

Equations associated with ideas:
 $q_{1}$ on $q_{p}$ (virtual)

magnitudes!
OR: equate the magnitudes

$$
E_{1, x}=+\frac{K g_{1}}{(L / 4)^{2}}
$$

$$
E_{2, x}=-\frac{K q_{2}}{(3 / 4 L)^{2}}
$$

$$
E_{\text {net }, x}=E_{1, x}+E_{2, x}=0
$$ vectorial addition.

$$
\begin{aligned}
& \vec{E}_{1}=\frac{1}{4 \pi \varepsilon_{0}} \frac{q_{1}}{r_{1}^{2}} \hat{r}_{1}
\end{aligned}
$$

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- This condition should constrain the ratio of the two charges. Name $q_{1}=R q_{2}$.
- Keep in mind: the same sign of $q_{1}$ and $q_{2}$ leads to zero net field.


## Solution

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$\frac{K q_{1}}{(L / 4)^{2}}=\frac{K q_{2}}{(3 L / 4)^{2}}, \quad K=\frac{1}{4 \pi \varepsilon_{0}}$

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- Note: $q^{2} \cdot q_{2}>0$ same sign is required, Note: $q_{1} \cdot q_{2}>0$ both can be negative

Electric fields from $q_{1}$ and $q_{2}$ at $A$ (i nbetween) point in opposite directions $\rightarrow$ cancellation is possible. Do not add $\frac{k q_{i}}{r_{i}^{2}}$ naively!

