

PhysicsTutor^{mh}

Induction

Giambattista 20.46-47

Problem:

- A solenoid of length 2.8 cm and diameter 0.75 cm is wound with 160 turns/cm, and carries current of 0.2 A. What is the flux through one of the windings?
- The current is now decreasing at a rate of 35 A/s, what is the induced EMF in one winding?
- What is the induced EMF in the entire solenoid?

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$$B_{\text{sol}} = N \frac{\mu_0 I}{l} = \mu_0 I \frac{N}{l} \quad l = \text{length of solenoid}$$



magnetic field strength inside solenoid
(derived from Ampère's law)

$$n = \frac{\text{number of windings}}{\text{length}} = \frac{N}{l}$$

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$$\Phi_M^{\text{one loop}} = B_{\text{sol}} \cdot A_{\text{loop}} (\cdot \cos(0))$$

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- A solenoid is idealized as a certain number of current loops of diameter d in series.
- The current loops create a magnetic field. This field permeates each loop, ie, there is magnetic flux through each loop.
- EMF is generated when the flux changes. In this way the solenoid counteracts rapid changes: electromagnets display inertia.

*magnetic flux from N -turn solenoid changes in one turn
→ EMF / turn , then add them in series
→ self inductance $L \sim N^2$!*

Equations associated with ideas:

$$B_{\text{sol}} = N \frac{\mu_0 I}{\ell}$$

$$\Phi_M^{(1)} = N \frac{\mu_0 I}{\ell} \pi \left(\frac{d}{2}\right)^2 \text{ in one turn}$$

$$\mathcal{E} = - \frac{\Delta \Phi_M}{\Delta t}$$

caused by $\frac{\Delta I}{\Delta t}$

$$\Phi_M^{(1)} = \frac{L I}{N}$$

(one turn)

$$\therefore L = \frac{N^2}{\ell} \mu_0 \pi \left(\frac{d}{2}\right)^2 \quad \text{(no iron core)}$$

self inductance in Henry

Flux for entire solenoid $\Phi_M = L I = N \Phi_M^{(1)}$

$$\text{Solenoid-EMF: } \mathcal{E}_{\text{sol}} = - \frac{\Delta \Phi_M}{\Delta t} = -L \frac{\Delta I}{\Delta t}$$

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- Calculate the rate of change of the flux from the rate of change for the current, deduce the EMF for one turn. Sum EMF from N windings.

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- $\Phi_M^{\text{sol}} = N \Phi_M^{(1)} = 7.9 \times 10^{-5} \text{ Wb} \quad \therefore L = \frac{\Phi_M^{\text{sol}}}{I} = 0.4 \text{ mH}$

$$\frac{\Delta \Phi_M^{\text{sol}}}{\Delta t} = L \frac{\Delta I}{\Delta t} = 0.4 \times 10^{-3} \text{ H} \cdot \left(-\frac{35 \text{ A}}{\text{s}}\right) \therefore \mathcal{E} = 0.014 \text{ V} = 14 \text{ mV}$$