

# PhysicsTutor<sup>mh</sup>

Interference

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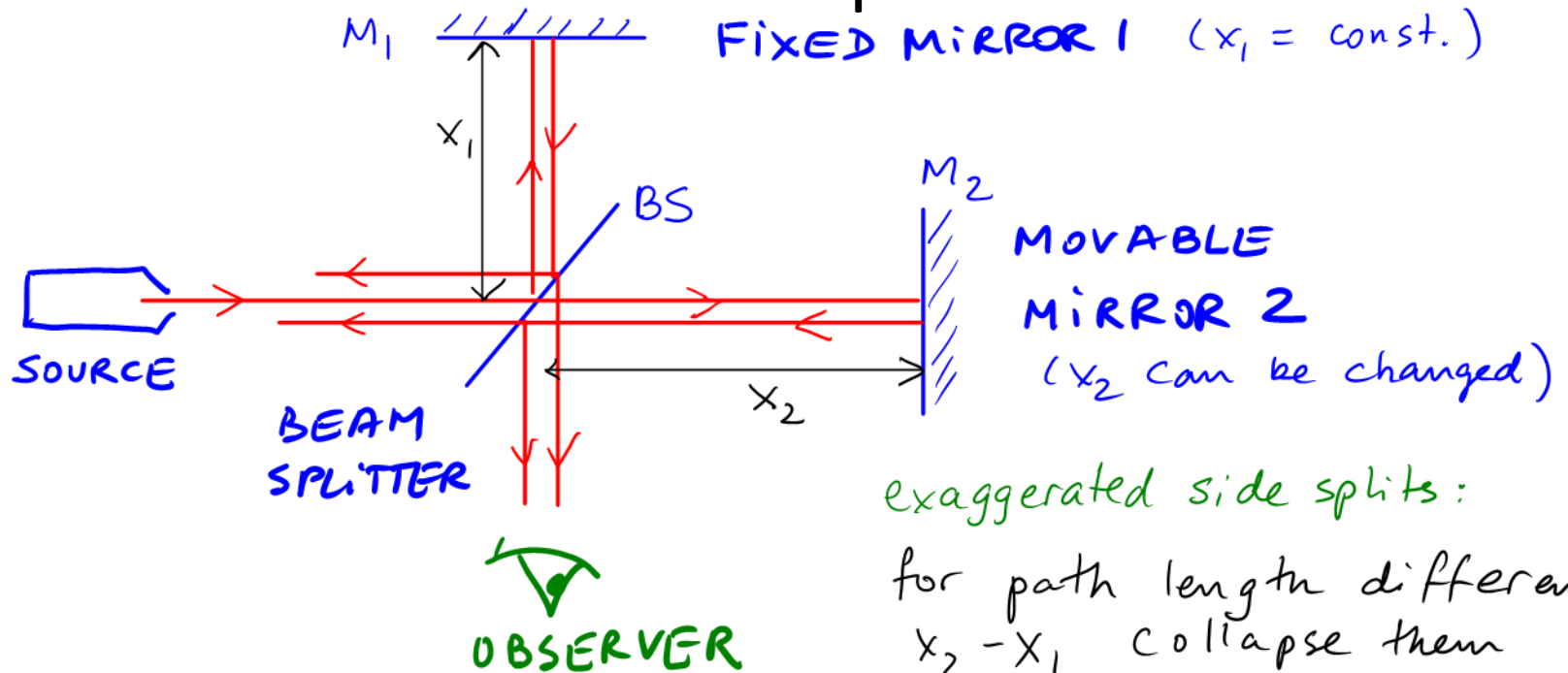
# Problem:

- One of the mirrors of a Michelson interferometer is moved a distance of 2.0 mm. Meanwhile, the interference intensity moves through 7,000 dark fringes.
- What is the wavelength of the light?

Relevant ideas:

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- Beams are split several times: the beam from the source is split in two, the returning beams from each mirror are also split.



exaggerated side splits:  
for path length difference  
 $x_2 - x_1$  collapse them  
into one!

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- The number of phase jumps is the same for recombining beams.

*beam 1 at BS and M1*

*beam 2 at M2 and BS*

# Relevant ideas:

- Beams are split several times: the beam from the source is split in two, the returning beams from each mirror are also split.
- The number of phase jumps is the same for recombining beams.
- Find the path length difference. Ignore the details about the glass beam splitter (front surface versus back surface reflections).

# Equations associated with ideas:

$$E_{1/2}(x, t) = E_0 \sin(\omega t - \frac{2\pi}{\lambda} x)$$

to be combined at same time  $t$  in the same place, but beam 2 accumulated more phase if  $x_2 > x_1$ :

$$\Delta\phi = \frac{2\pi}{\lambda} \Delta x \quad \text{where } \Delta x = 2(x_2 - x_1); \lambda = \lambda_{\text{air}}$$
$$\lambda_{\text{air}} = \lambda_{\text{vac}} / n_{\text{air}} \quad n_{\text{air}} \approx 1$$

$$\Delta\phi = (2m - 1)\pi \quad \text{destructive interference condition}$$

$m = 1, 2, \dots$   
crest meets trough  $\rightarrow$  dark

$$m = 7000 \quad \hat{=} \quad x_2 - x_1 = 2.0 \text{ mm} = \frac{\Delta x}{2} !$$

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- Same arrival time for both paths: find the accumulated phase difference (PD) in space from the optical path length difference.
- Equate the PD to an odd-integer multiple of  $\pi$  for destructive interference.
- Use the order  $m=7000$  to find  $\lambda$ .

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- $$\lambda = 0.571 \mu\text{m} \rightarrow 570 \text{ nm} \rightarrow \text{yellow light} \checkmark$$

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Our calculation was based upon the path length difference between arms 1 and 2. The problem did not state that the path length was the same initially (constructive interference), but fringes appear/disappear proportional to the change in path length.