## PhysicsTutor

Polarizer

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## Problem:

- Unpolarized light with electric field amplitude $0.25 \mathrm{~V} / \mathrm{m}$ is incident on a polarizer.
- Calculate the electric field amplitude of the transmitted light.


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- Intensity is prop. to E field strength squared.

Equations associated with ideas:

Malus:

$$
\begin{aligned}
& I(\varphi)=I_{0} \cos ^{2} \varphi \\
& E(\varphi)=E_{0} \cos \varphi
\end{aligned}
$$



Allow all orientations $\varphi$
Average $I(\varphi)$ over $\varphi$ :

$$
\begin{aligned}
& I_{\text {arg }}=\frac{1}{\pi} \int_{0}^{\pi} d \varphi I(\varphi)=\frac{I_{0}}{\pi} \int_{0}^{\pi} \underbrace{\cos ^{2} \varphi}_{=\frac{1}{2}(1+\cos 2 \varphi)} d \varphi=\frac{I_{0}}{2 \pi}\left(\int_{0}^{\pi} d \varphi+\int_{0}^{\pi} \cos 2 \varphi d \varphi\right) \\
& \text { average definition } \\
& \cos _{4}^{2} \varphi \text { box } \\
& \text { divible } \\
& \text { base length } \\
& \text { to set } \square \text { height } \\
& \text { from area } \\
& \text { or "see if" by looking } \\
& \text { at a careful graph, }
\end{aligned}
$$

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- Take the root to obtain the E field strength.


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after polarizer
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$E^{\text {after polarizer }} \sim \sqrt{\frac{I_{0}}{2}}=0.177 \frac{\mathrm{~V}}{\mathrm{~m}}=0.18 \frac{\mathrm{~V}}{\mathrm{~m}}$
The polarizes is NOT selecting a subset of wares with $\vec{E}$ aligned with its axis. All but the perpendicular $\vec{E}$-directions do contribute. That we obtain half the original intensity for this polarizer orientation, and another half if the polarizer were rotated by $\pi / 2$ should make sense.

