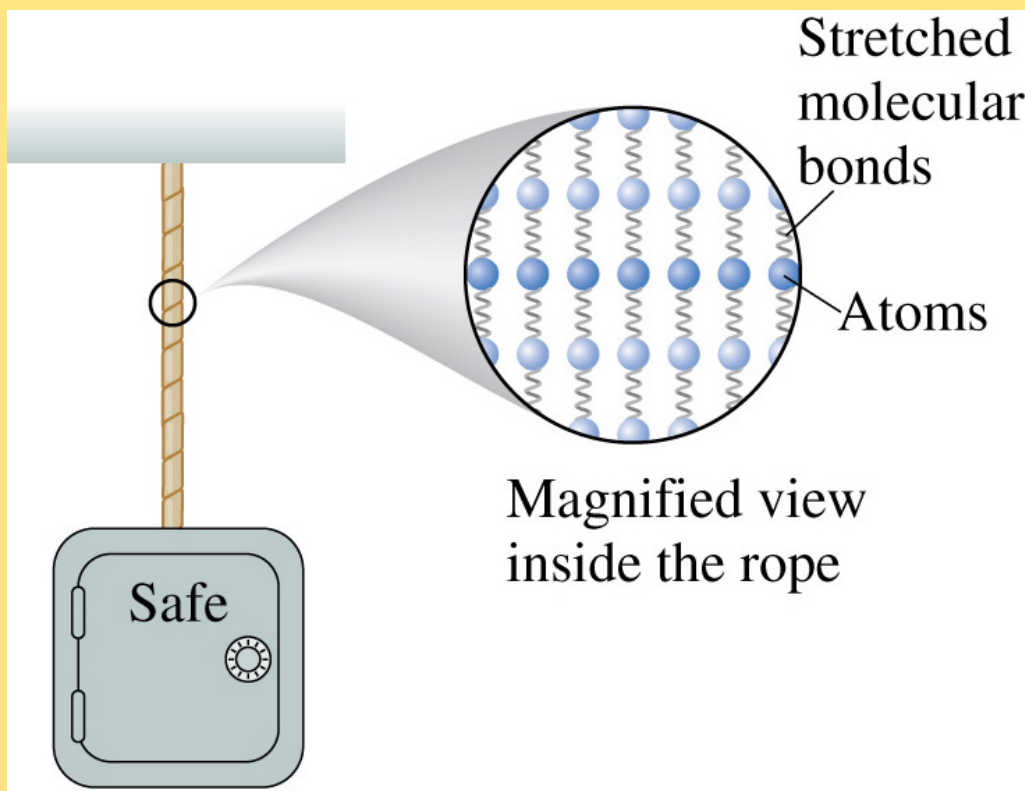
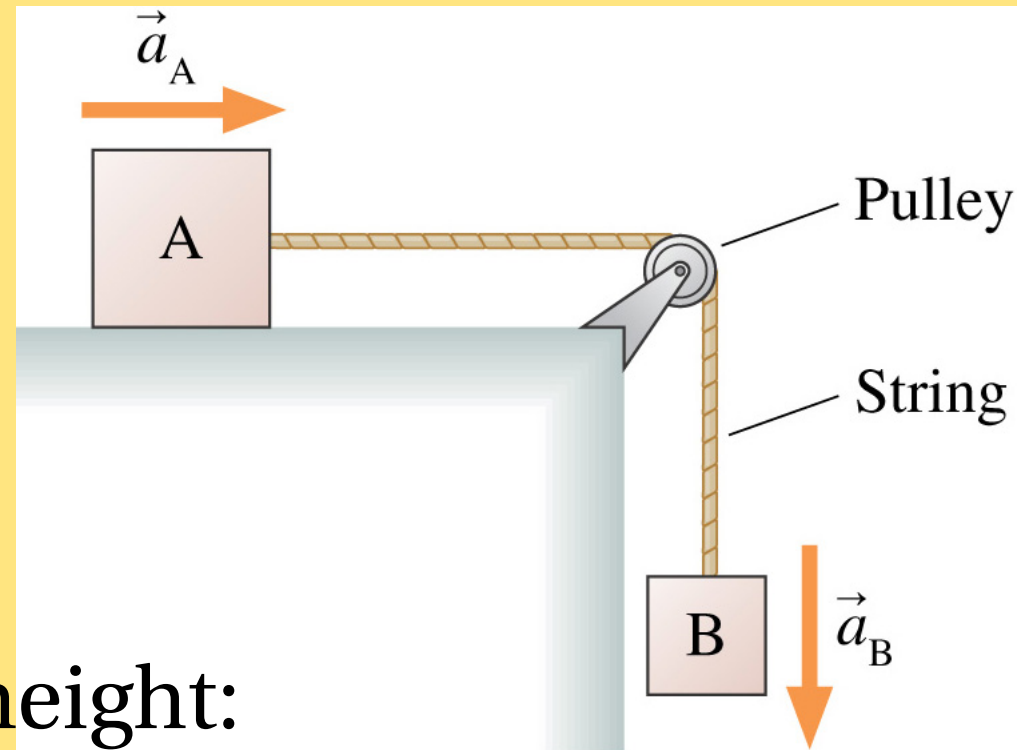


# Ropes and Pulleys

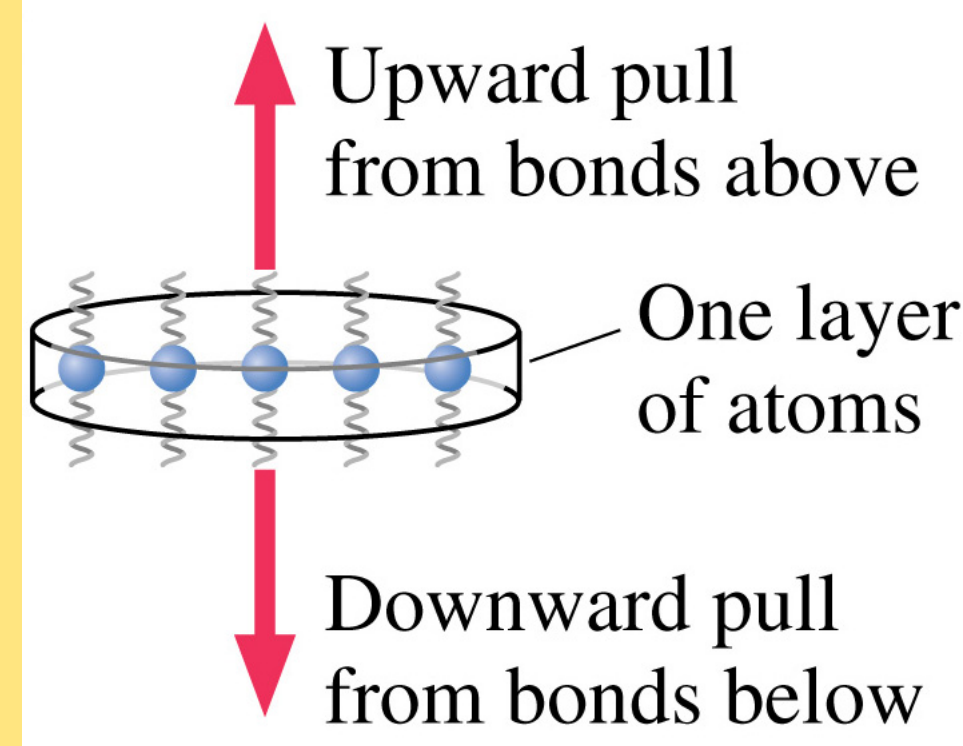
Non-stretching string and pulley:  
re-direct acceleration vectors

To understand strings (ropes):  
re-visit tension force



Cut rope at any height:  
mass falls!  $\Rightarrow$   
tension is  
everywhere!

$\infty$ -ly many  
free-body  
diagrams?



No, assume the string to be massless

Rope transmits the same tension force from one end to the other

Not meaningful to apply Newton's 2nd to a layer of  $m = 0$  atoms

Bond springs are ultra-stiff (huge  $k$ )  $\Rightarrow$  tiny displacement

# Moving Ropes

Suppose a crane can lower/heighten the load attached to the rope.

What is the tension force if the mass is accelerated upward by  $\vec{a}$ ?

$|\vec{w}_{E \text{ on } S}| = |\vec{T}_{R \text{ on } S}|$  only holds when S is at rest, or moves with constant velocity  
Newton's 2<sup>nd</sup>:

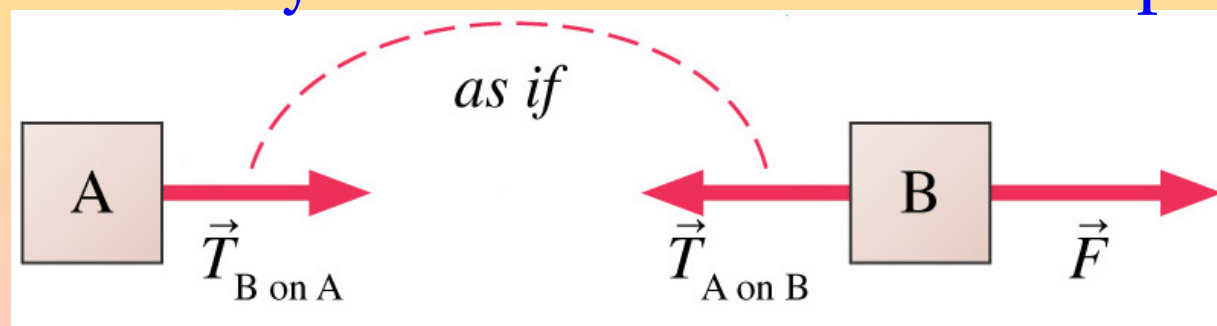
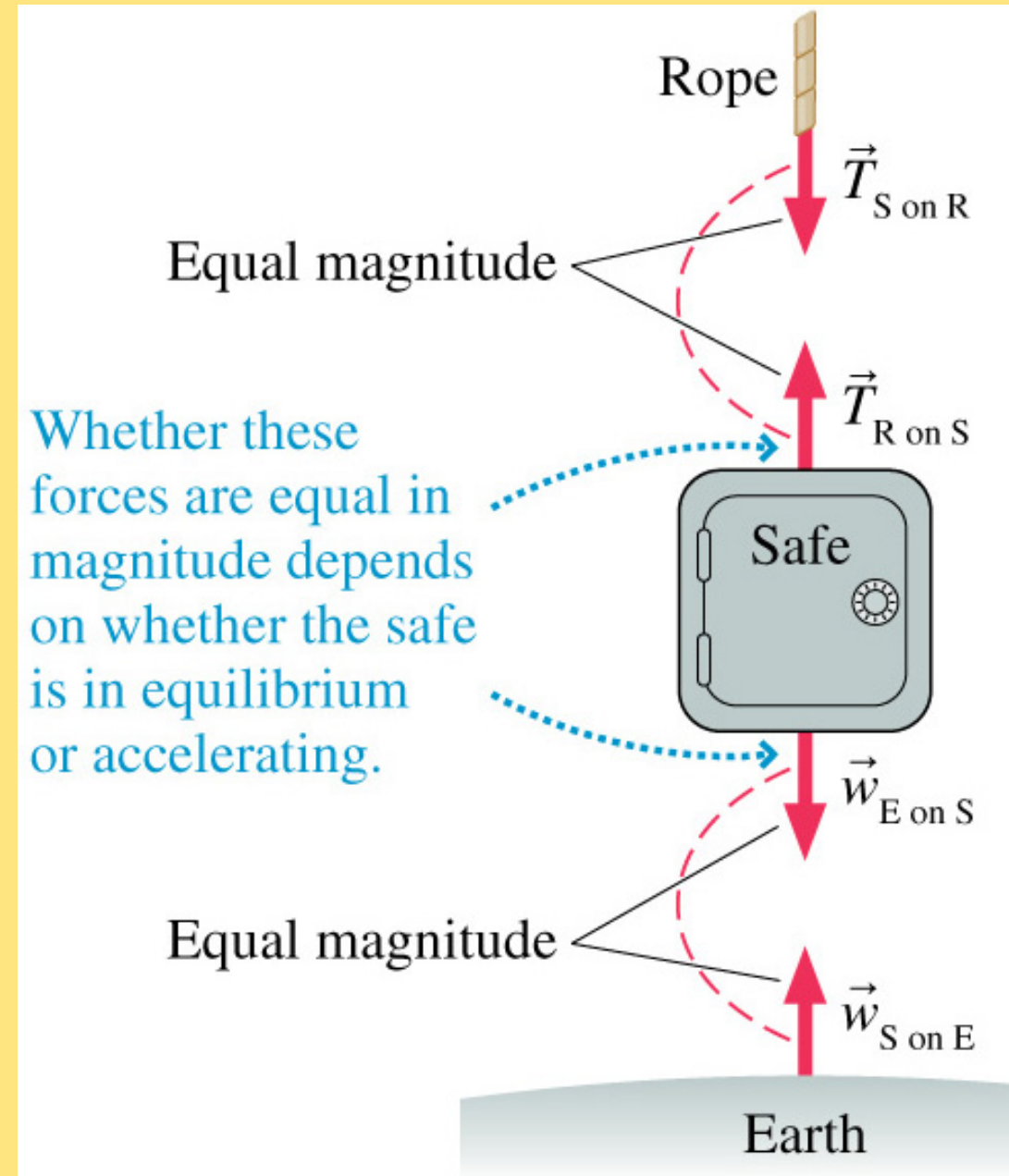
If  $a_S \neq 0$ , then from  $m_S \vec{a}_S = \vec{F}_{S,\text{net}}$  it follows that  $\vec{F}_{S,\text{net}} = \vec{T}_{R \text{ on } S} + \vec{w}_{E \text{ on } S}$

**Moral:** suppose a rope is rated for a maximum tension force just above  $m_S g$ .

What happens when the crane (towing car) accelerates like mad?

What if the car to be towed left the emergency brake on?

Important short-cut for massless strings: treat tension forces at ends as if they were an action-reaction pair, and ignore the string.



This also works when the string bends around by moving over a pulley, at least in the massless pulley approximation