

Kinetic Theory of Gases: Assumptions

- 1. A gas is made up of a large number of extremely small particles (molecules or atoms) in constant, random, straight line motion
- 2. Molecules occupy very little volume (most of the container is free space)
- 3. Molecules collide with one another and with the walls of the container
- 4. There are no forces between the molecules
- 5. Molecules can gain or lose energy on collision but the total energy remains constant

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The theory will give information on the speeds of molecules, the frequency with which they collide, and the distribution of energy

It is only useful if it can predict the gas laws

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Pressure comes from the gas molecules hitting the walls of the container. Hence if we can determine the force with which the molecules hit the wall we can determine the pressure.

Suppose you have a gas with N identical molecules of mass m in a container of volume V. Also assume that each molecule has

a speed u, but that it can be different for different molecules.

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$$P = \frac{1}{3} \frac{Nm \ \overline{u^2}}{V} \qquad \therefore PV = \frac{1}{3} \frac{Nm \ \overline{u^2}}{V}$$

This is looking a lot like PV = constant

If $\overline{u^2}$ is a constant at constant temperature.

This is Boyle's Law

We will not prove this but assume it is true and use the PV equations from the macroscopic and microscopic sections to learn about speed and temperature

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Temperature/kinetic energy/speedThe kinetic energy of a molecule is: $\frac{1}{2}mu^2$ The average kinetic energy of a molecule is: $\frac{1}{2}mu^2$ The kinetic energy of a mole of molecules is $\frac{1}{2}N_Amu^2$ (N_A is Avogadro's number)CHEM 1000 30

The kinetic energy of a mole of molecules (E) is

$$E = \frac{1}{2} N_A m \overline{u^2} \quad \therefore \quad m \overline{u^2} = \frac{2E}{N_A}$$
But

$$PV = \frac{1}{3} \frac{Nm \overline{u^2}}{u^2} = \frac{2}{3} \frac{N.E}{N_A} = \frac{2}{3} \frac{n.E}{3}$$
given that

$$PV = nRT$$

$$nRT = \frac{2}{3} \frac{n.E}{M_A} \quad \therefore \quad E = \frac{3}{2} RT$$
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	peed greater th	Fraction of molecules with speeds greater than u
	0	1 (all molecules go faster than 0)
	3u _m	4.5x10 ⁻⁴
	5u _m	4x10 ⁻¹⁰
	10u _m	4x10 ⁻⁴³
Мо	st molecules h	ave speeds close to u _m

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Collisions with the Wall

The number of collisions that molecules make with the wall depend on how many molecules there are (per unit volume) and how fast they are moving. Z_{wall} will have units of m⁻² s⁻¹

$$Z_{\text{wall}} \propto \frac{N}{V} \cdot u_{\text{av}}$$
 actually $Z_{\text{wall}} = \frac{1}{4} \frac{N}{V} \cdot u_{\text{av}}$

Effusion

We can obtain a quantitative understanding of effusion by recognizing that effusion is the loss of a molecule that would normally hit the wall.

$$Z_{\text{wall}} = \frac{1}{4} \frac{N}{V} \cdot u_{\text{a}}$$

The rate at which molecules leave the container is the wall collision rate times the area of the hole

Rate of effusion =
$$Z_{wall} \cdot A = \frac{1}{4} \frac{N}{V} \cdot u_{av} \cdot A$$

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$$\therefore \text{ for 2 gases (A and B) in the same container}}$$

$$\frac{\text{rate of effusion of A}{\text{rate of effusion of B}} = \frac{Z_{wall}(A).A}{Z_{wall}(B).A} = \frac{\frac{1}{4} \frac{N_A}{V} .u(A)_{av}.A}{\frac{1}{4} \frac{N_B}{V} .u(B)_{av}.A}$$

$$= \frac{N_A}{N_B} \frac{u(A)_{av}}{u(B)_{av}} = \frac{N_A}{N_B} \frac{\sqrt{8RT/\pi M_A}}{\sqrt{8RT/\pi M_B}} = \frac{N_A}{N_B} \frac{\sqrt{M_B}}{\sqrt{M_A}}$$
Note that the ratio of the number of molecules is the ratio of the partial pressures
$$\frac{\text{rate of effusion of A}}{\text{rate of effusion of B}} = \frac{P_A}{P_B} \frac{\sqrt{M_B}}{\sqrt{M_A}}$$
and for EQUAL pressures
$$\frac{\text{rate of effusion of A}}{\text{rate of effusion of B}} = \frac{\sqrt{M_B}}{\sqrt{M_A}} \quad \text{Graham's Law}$$
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Collisions between molecules

When studying interactions between gas molecules you need to know how often the molecules actually collide

The collision frequency is the number of collisions a particular molecule makes in one second. This will depend on how many molecules there are (per unit volume), how fast they are moving, and how big they are.

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Mean free path

A related parameter is the average distance a molecule travels between collisions. This is the mean free path

The collision frequency is $Z_A s^{-1}$

The time between collisions is $1/Z_A$ s

The average speed of the molecules is \boldsymbol{u}_{av}

Since distance is speed times time

$$\lambda = \frac{u_{av}}{Z_A} = \frac{1}{\sqrt{2}\pi d^2} \frac{V}{N}$$
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