

$$N_T = N_0 \cdot 2^{(T/g)}$$

as time increases,  $t/g = 1, 2, 3 \dots$ , thus  $2^1, 2^2, 2^3$ , etc.  
 $g$  is the generation time  
 $N_0$  is the number of cells at time  $T = 0$   
 $N_T$  is the number of cells at time  $T$

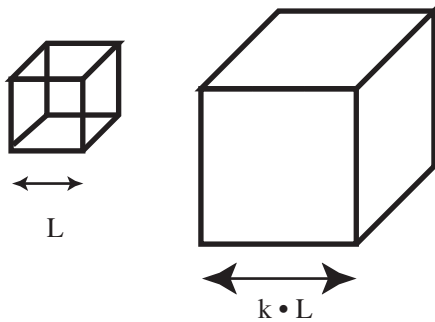
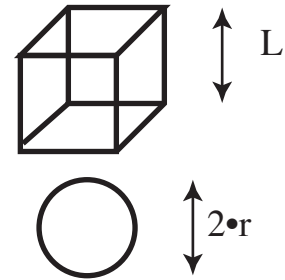
Logistic growth curve:

$$N_T = \frac{K \cdot N_0 \cdot e^{T/g}}{K + N_0(e^{T/g} - 1)}$$

$K$  is the carrying capacity

A cube has a surface area of  $6 \cdot L^2$ . Its volume is  $L^3$ . As long as the shape is constant, the ratio of surface area to volume will always be  $(6 \cdot L^2) / L^3$ , or  $6/L$ .

For a sphere, the surface area is  $4 \cdot \pi \cdot r^2$ , and the volume is  $\pi \cdot r^3$ ; the corresponding ratio of surface area to volume is  $4/r$ .



(area)  $A_1 = 6 \cdot L^2$        $A_k = 6 \cdot (k \cdot L)^2$        $A_k = 6 \cdot k^2 \cdot L^2$  (  $= k^2 \cdot A_1$  )  
 (volume)  $V_1 = L^3$        $V_k = (k \cdot L)^3$        $V_k = k^3 \cdot L^3$  (  $= k^3 \cdot V_1$  )  
 The scaling coefficient is different for area ( $k^2$ ) and for volume ( $k^3$ ).

Heat conduction rates are defined by the relation:  $P_{\text{cond}} = Q / t = k \cdot A \cdot [(T_a - T_b) / L]$  where  $P_{\text{cond}}$  is the rate of conduction (transferred heat,  $Q$ , divided by time,  $t$ );  $k$  is the thermal conductivity;  $T_a$  and  $T_b$  are the temperatures of the two heat reservoirs  $a$  and  $b$ ;  $A$  is the area; and  $L$  is the distance. Thermal conductivities of water and air are about  $0.6$  and  $0.024 \text{ W m}^{-1} \text{ K}^{-1}$ , respectively.

Thermal radiation is defined by the relation:  $P_{\text{rad}} = \sigma \cdot \epsilon \cdot A \cdot T^4$

where  $P_{\text{rad}}$  is the rate of radiation;  $\sigma$  is the Stefan-Boltzmann constant ( $5.6703 \cdot 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$ );  $\epsilon$  is the emissivity (varies from  $0$  to  $1$ , where  $1$  is for a blackbody radiator);  $A$  is the area; and  $T$  is the temperature (in Kelvins). The *net* radiative emission or absorption will depend upon the difference in temperature:  $P_{\text{net}} = \sigma \cdot \epsilon \cdot A \cdot (T_{\text{body}}^4 - T_{\text{ambient}}^4)$

$$\text{compression} = \rho \cdot h \quad F_{cr} = \frac{E \cdot I \cdot \pi^2}{L_{\text{eff}}^2} \quad \Psi_{wv} = \frac{RT}{\bar{V}_w} \ln\left(\frac{\% \text{ relative humidity}}{100}\right) + \rho_w g h$$

$$F_{cr} = \frac{E \cdot \pi \cdot r}{(2 \cdot h)^2} \cdot \pi^2, \text{ and } F_{cr} = \rho \cdot \pi \cdot r^2 \cdot h$$

velocity (meters sec<sup>-1</sup>)    pressure difference (Pascal = 1 kg m<sup>-1</sup> sec<sup>-1</sup>)    tube radius    density (water = 1 gm cm<sup>-3</sup>)

$$v = \left( \frac{\Delta p}{l} \right) \left( \frac{1}{4 \cdot \eta} \right) (R^2 - r^2)$$

distance (meters)    distance from center of tube    viscosity (water = 0.01 gm cm<sup>-1</sup> sec<sup>-1</sup>, or Pa sec)

velocity (cm sec<sup>-1</sup>)    tube diameter (cm)

$$R_e = \frac{\rho \cdot v \cdot l}{\eta}$$

viscosity (water = 0.01 gm cm<sup>-1</sup> sec<sup>-1</sup>)

$$v = \left( \frac{\Delta p}{l} \right) \left( \frac{1}{4 \cdot \eta} \right) R^2$$

$$J_v = \left( \frac{\Delta p}{l} \right) \left( \frac{\pi}{8 \cdot \eta} \right) \cdot R^4$$

$$J_v = - \frac{r^2}{8 \cdot \eta} \cdot \frac{\partial P}{\partial x}$$

$$J = -D \frac{\partial c}{\partial x}$$

Fick's First Law of Diffusion: The flux is proportional to the concentration gradient

$$\frac{\partial c}{\partial t} = D \frac{\partial^2 c}{\partial x^2}$$

$$\frac{\partial c}{\partial t} = - \frac{\partial J}{\partial x}$$

Fick's Second Law of Diffusion: Changes in concentration over time depend upon the flux gradient

$$J = - \frac{1}{2} \cdot \frac{\Delta^2}{\tau} \cdot \frac{dC}{dx}$$

$$\nabla v = u \frac{\partial}{\partial x} + v \frac{\partial}{\partial y} + w \frac{\partial}{\partial z}$$

$$D = \frac{1}{2} \cdot \frac{\Delta^2}{\tau}$$

velocity vector — the notation grad v is sometimes used

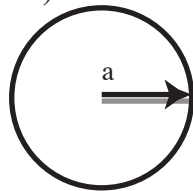
with velocity components, u, v, and w, in the three dimensions, x, y, and z.

units: moles cm<sup>-2</sup> sec<sup>-1</sup>

$$J_x = -D \frac{\partial c}{\partial x} + v_x \cdot c$$

(cm<sup>2</sup> sec<sup>-1</sup>)(moles cm<sup>-4</sup>)    (cm sec<sup>-1</sup>)(moles cm<sup>-3</sup>)

Fick's First law :  $J_r = -D \frac{\partial C}{\partial r}$



Fick's Second Law :  $\frac{\partial C}{\partial t} = D \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \frac{\partial C}{\partial r} \right) = 0$

$$C(r) = C_0 \left( 1 - \frac{a}{r} \right)$$

(steady state)

$$J_r(a) = -D \cdot C_0 \cdot 4 \cdot \pi \cdot a = I_D \quad (\text{diffusive current})$$

(units of mole sec<sup>-1</sup>)  
(mole cm<sup>-2</sup> sec<sup>-1</sup>)

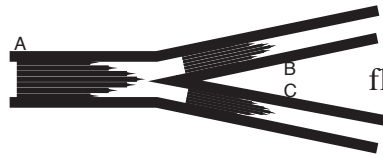
$$P_e = \frac{2 \cdot a \cdot u}{D}$$

$$I_m = 4 \cdot \pi \cdot a^2 \cdot \beta \quad (\text{metabolic current})$$

(cm<sup>2</sup>)      (units of mole sec<sup>-1</sup>)

$$\frac{\partial C}{\partial t} = u \cdot \frac{\partial C}{\partial r} \cdot C + D \frac{\partial^2 C}{\partial r^2}$$

$$Q = \frac{\Delta p \pi a^4}{l 8 \eta}$$



flow velocity

concentration gradient

concentration

$$\mu_j^{liquid} = \mu_j^* + RT \ln a_j + \bar{V}_j P + z_j F E + m_j g h$$

$$D = \frac{1}{2} \cdot \rho \cdot V^2 \cdot A \cdot C_D$$

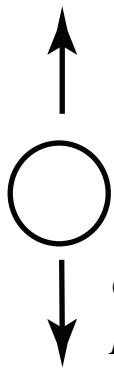
fluid density      velocity  
frontal area      drag coefficient  
(shape-dependent)

$$m \left( -\frac{dv}{dt} \right) = 6 \cdot \pi \cdot \eta \cdot r \cdot v$$

(  $-\frac{6 \cdot \pi \cdot \eta \cdot r \cdot t}{m}$  )

$$v(t) = v_0 e$$

$$V_{\text{terminal}} = \sqrt{\frac{2mg}{\rho A C_D}}$$



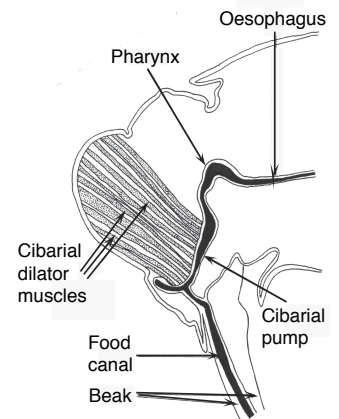
Frictional force  
 $F_f = 6\pi\eta a v$

Where the frictional and gravitational forces are balanced, the velocity reaches a steady state.

Gravitational pull  
 $F_g = \frac{4}{3} \pi a^3 \Delta \rho g$

The energetic details of the pumping mechanism are shown below for *Rhodnius* (a blood sucking insect) and spittlebugs (*Philaenus*)<sup>[1]</sup>.

	<i>Rhodnius</i>	<i>Philaenus</i>
Muscle tension (maximum)	600 kPa	600 kPa
Pump stroke frequency	3 Hz	1.7 Hz
Muscle contraction rate (muscle lengths per second)	1 s <sup>-1</sup>	0.5 s <sup>-1</sup>
Ratio of muscle/piston	2.5	10.0
Maximum muscle tension	-300 kPa	-2400 kPa



Symbol	Value	Units	Comments
<b>GAS CONSTANT</b>			
R	8.314	J mol <sup>-1</sup> K <sup>-1</sup>	R is the Boltzmann constant times Avogadro's Number (6.023•10 <sup>23</sup> )
	1.987	cal mol <sup>-1</sup> K <sup>-1</sup>	
	8.314	m <sup>3</sup> Pa mol <sup>-1</sup> K <sup>-1</sup>	
RT	2.437 • 10 <sup>3</sup>	J mol <sup>-1</sup>	At 20 °C (293 °K)
	5.833 • 10 <sup>2</sup>	cal mol <sup>-1</sup>	At 20 °C (293 °K)
	2.437	liter MPa mol <sup>-1</sup>	At 20 °C (293 °K)
RT/F	25.3	mV	At 20 °C (293 °K)
2.303 • RT	5.612	kJ mol <sup>-1</sup>	At 20 °C (293 °K)
	1.342	kcal mol <sup>-1</sup>	At 20 °C (293 °K)
<b>FARADAY CONSTANT</b>			
F	9.649 • 10 <sup>4</sup>	coulombs mol <sup>-1</sup>	F is the electric charge times Avogadro's Number
	9.649 • 10 <sup>4</sup>	J mol <sup>-1</sup> V <sup>-1</sup>	
	23.06	kcal mol <sup>-1</sup> V <sup>-1</sup>	
<b>CONVERSIONS</b>			
kcal	4.187	kJ (kiloJoules)	Joules is an energy unit (equal to 1 Newton•meter)
Watt	1	J sec <sup>-1</sup>	
Volt	1	J coulomb <sup>-1</sup>	
Amperes	1	coulomb sec <sup>-1</sup>	
Pascal (Pa)	1	Newton meter <sup>-2</sup>	Pascal is a pressure unit (equal to 10 <sup>-5</sup> bars)
Siemens	1	Ohm <sup>-1</sup>	Siemens (S) is conductance, the inverse of resistance (Ohm)
<b>PHYSICAL PROPERTIES</b>			
η <sub>w</sub>	1.004 • 10 <sup>-3</sup>	Pa sec	viscosity of water at 20 °C
ν <sub>w</sub>	1.004 • 10 <sup>-6</sup>	m <sup>2</sup> sec <sup>-1</sup>	kinematic viscosity of water at 20 °C (viscosity/density)
V <sub>w</sub>	1.805 • 10 <sup>-5</sup>	M <sup>3</sup> mol <sup>-1</sup>	Partial molal volume of water at 20 °C (viscosity/density)

Source: Nobel, Park S (1991) Physicochemical and Environmental Physiology