

# 13

# Newton's Theory of Gravity

## 13.1 A Little History

## 13.2 Isaac Newton

## 13.3 Newton's Law of Gravity

1. Is the earth's gravitational force on the moon larger than, smaller than, or equal to the moon's gravitational force on the earth? Explain.

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2. Star A is twice as massive as star B. They attract each other.

- a. Draw gravitational force vectors on both stars. The length of each vector should be proportional to the size of the force.



$m_A = 2m_B$



$m_B$

- b. Is the acceleration of star A larger than, smaller than, or equal to the acceleration of star B? Explain.

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3. The gravitational force of a star on orbiting planet 1 is  $F_1$ . Planet 2, which is twice as massive as planet 1 and orbits at half the distance from the star, experiences gravitational force  $F_2$ . What is the ratio  $F_2/F_1$ ?

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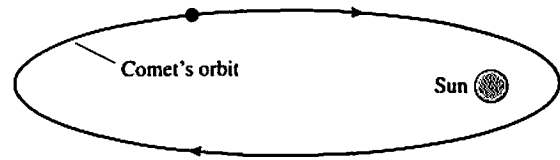
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4. Comets orbit the sun in highly elliptical orbits. A new comet is sighted at time  $t_1$ .



- a. Later, at time  $t_2$ , the comet's acceleration  $a_2$  is twice as large as the acceleration  $a_1$  it had at  $t_1$ . What is the ratio  $r_2/r_1$  of the comet's distance from the sun at  $t_2$  to its distance at  $t_1$ ?

- b. Still later, at time  $t_3$ , the comet has rounded the sun and is headed back out to the farthest reaches of the solar system. The size of the force  $F_3$  on the comet at  $t_3$  is the same as the size of force  $F_2$  at  $t_2$ , but the comet's distance from the sun  $r_3$  is only 90% of distance  $r_2$ . Astronomers recognize that the comet has lost mass. Part of it was "boiled away" by the heat of the sun during the time of closest approach, thus forming the comet's tail. What percent of its initial mass did the comet lose?

### 13.4 Little $g$ and Big $G$

5. How far away from the earth does an orbiting spacecraft have to be in order for the astronauts inside to be weightless?

6. The free-fall acceleration at the surface of planet 1 is  $20 \text{ m/s}^2$ . The radius and the mass of planet 2 are half those of planet 1. What is  $g$  on planet 2?

## 13.5 Gravitational Potential Energy

7. Explain *why* the gravitational potential energy of two masses is negative. Note that saying “because that’s what the formula gives” is *not* an explanation. An explanation makes use of the basic ideas of force and potential energy.

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## 13.6 Satellite Orbits and Energies

8. Planet X orbits the star Alpha with a “year” that is 200 earth days long. Planet Y circles Alpha at nine times the distance of planet X. How long is a year on planet Y?

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9. The mass of Jupiter is  $M_{\text{Jupiter}} = 300M_{\text{earth}}$ . Jupiter orbits around the sun with  $T_{\text{Jupiter}} = 11.9$  years in an orbit with  $r_{\text{Jupiter}} = 5.2r_{\text{earth}}$ . Suppose the earth could be moved to the distance of Jupiter and placed in a circular orbit around the sun. The new period of the earth’s orbit would be
- |   |   |
|---|---|
| a. 1 year.  | b. 11.9 years.  |
| c. Between 1 year and 11.9 years.                                   | d. More than 11.9 years.  |
| e. It could be anything, depending on the speed the earth is given. | f. It is impossible for a planet of earth’s mass to orbit at the distance of Jupiter. |

Circle the letter of the true statement. Then explain your choice.

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10. Satellite A orbits a planet with a speed of 10,000 m/s. Satellite B is twice as massive as satellite A and orbits at twice the distance from the center of the planet. What is the speed of satellite B?

11. a. A crew of a spacecraft in a clockwise circular orbit around the moon wants to change to a new orbit that will take them down to the surface. In which direction should they fire the rocket engine? On the figure, show the exhaust gases coming out of the spacecraft.
- b. On the figure, show the spacecraft's orbit after firing its rocket engine.
- c. The moon has no atmosphere, so the spacecraft will continue unimpeded along its new orbit until either firing its rocket again or (ouch!) intersecting the surface. As it descends, does its speed increase, decrease, or stay the same? Explain.

