

Guide to: Solenoid or coil, with or without iron core; also: any wire.

Applications: Oscillator circuits (transmitters/receivers). Transformers (mutual inductance).

Basic idea: Electrical current flow implies a magnetic field, which has energy content. This cannot be turned on/off instantly. Iron cores are magnetized by the field, and act to increase the overall field significantly (application: electromagnets).

Derivations: Faraday's law relates voltage drop (generated EMF) to magnetic flux change:  $\mathcal{E} = -\frac{d\Phi_B}{dt}$ .  
 For a solenoid (coil) the flux change comes from ramping up/down an electric current:

Solenoid of length  $X$  generates field:  $B = \frac{\mu_0 N I}{X}$ ; Flux through **one** turn:  $\Phi_B = B A = \frac{\mu_0 N I A}{X}$ .

Thus, the voltage drop is proportional to the rate of change of current [this looks a bit unusual].

$$\mathcal{E} = - \left( \frac{\mu_0 N^2 A}{X} \right) \frac{dI}{dt} \equiv -L \frac{dI}{dt}$$

. Extra factor of  $N$  comes from adding the loop-EMF in series.

The inductance is a 'material property' of the wire/coil/solenoid, and depends on its geometry (length  $X$  and cross sectional area  $A$ ). With iron core: multiply the expression for  $L$  by the relative permeability value for the core material; variable positioning of the core in/out of coil creates a variable inductor.

A tricky aspect in an  $N$ -turn coil/solenoid: flux change in a single turn is considered, then the turns connected in series result in  $N$  times the result. Since the magnetic field from  $N$  turns was added up, and entered the flux expression, the overall result depends on the square of  $N$ .

Equations:  $L = \frac{\mu_0 N^2 A}{X}$  with core:  $L = \frac{\mu_r \mu_0 N^2 A}{X}$ .

Parallel inductors:  $\frac{1}{L_{eq}} = \frac{1}{L_1} + \frac{1}{L_2} + \dots$ . Time constant:  $\tau = \frac{L}{R}$  exponential turn-on and off!

Unit: henry = volt.second/ampere . Voltage drop:  $\Delta V_L = -L \frac{dI}{dt}$

Problems: 21.30-45 and circuit problems 21.62-66

Understand the exponential turn-on and turn-off of currents (Fig. 21.22 in Giordano).

A simple wire (not a coil) also has inductance (complicated formula, requires calculus), and has resistance; thus no circuit can be turned on or off instantly!